

# PINGU and the Neutrino Mass Hierarchy

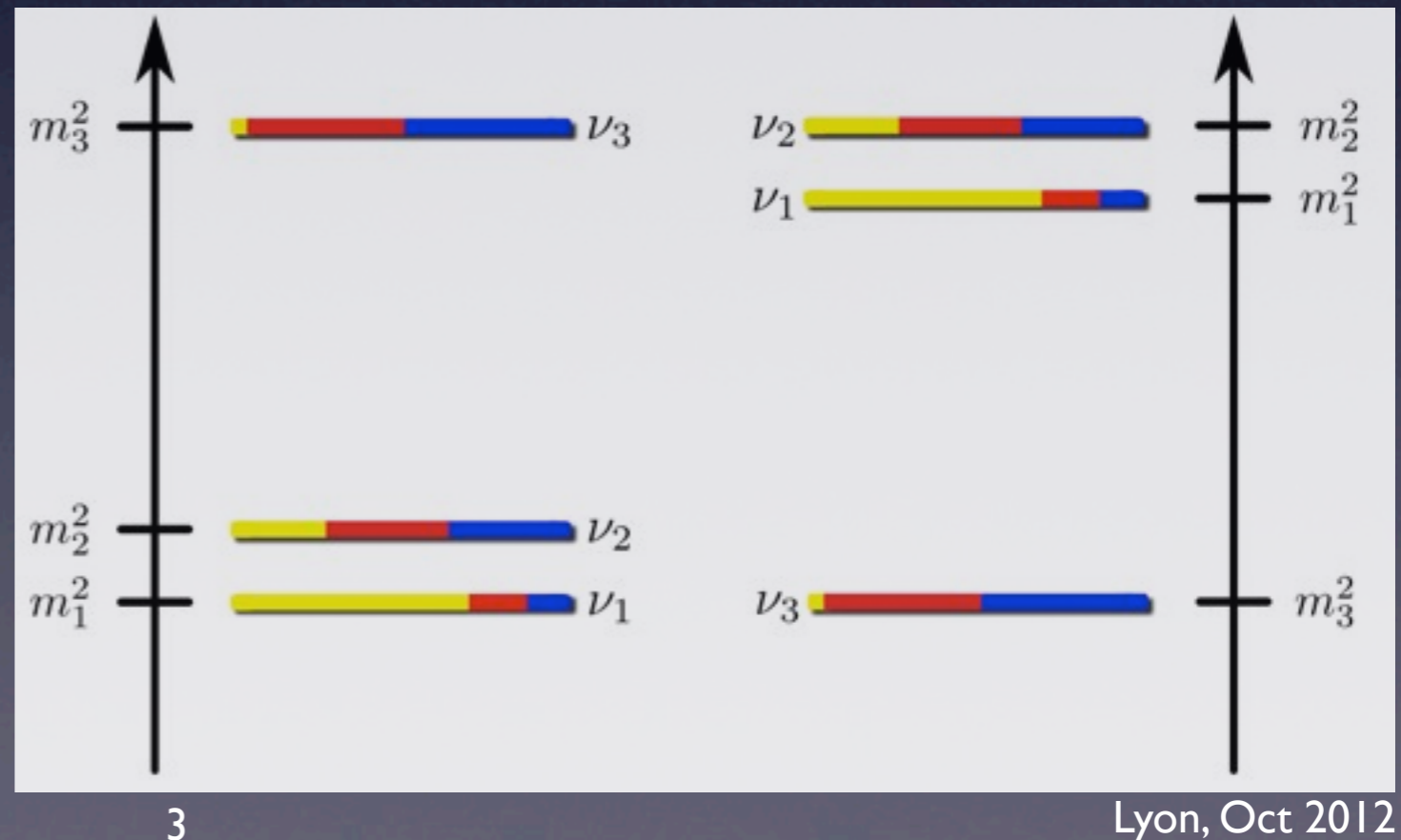
Ken Clark, Penn State University  
Neutrinos at the Forefront - Lyon, Oct 2012

# Neutrino Oscillations

- Neutrino oscillations parametrized by
  - mass squared differences  $\Delta m^2_{ij}$
  - mixing angles  $\theta_{ij}$
  - CP phase  $\delta_{CP}$
- Several questions remain
  - What is the mass hierarchy ( $m_3 > m_1$ ?)

# Neutrino Mass Hierarchy

- Focus on the mass hierarchy in this talk
- We know  $\Delta m^2_{13}$  but not the sign



# Experiments

- Several experiments targeting the mass hierarchy
- NOvA to start data collection soon
- R&D ongoing on Daya Bay II, LBNE, GLACIER, LENA, ORCA, PINGU

# Theory - Atmospheric Neutrinos

- Why use atmospheric neutrinos?
  - Not usually considered for use in precision parameter determination
- Broad range of baselines ( $\sim 50 - 12500$  km)
- Broad range of energies ( $\sim \text{GeV} - \text{PeV}$ )

# Theory

- Case for atmospheric neutrinos has been studied previously (Phys. Rev. D 78, 093003 (2008) in particular although there are others)
- In essence this requires distinction between normal and inverted hierarchy in counts
- Hierarchy effects seen as neutrinos pass through matter
  - $\nu$  oscillation probability is enhanced if hierarchy is normal
  - $\bar{\nu}$  oscillation probability is enhanced if hierarchy is inverted
  - and:  $\nu, \bar{\nu}$  have different cross sections
- Matter effects depend on size of  $\theta_{13}$  which is now better defined

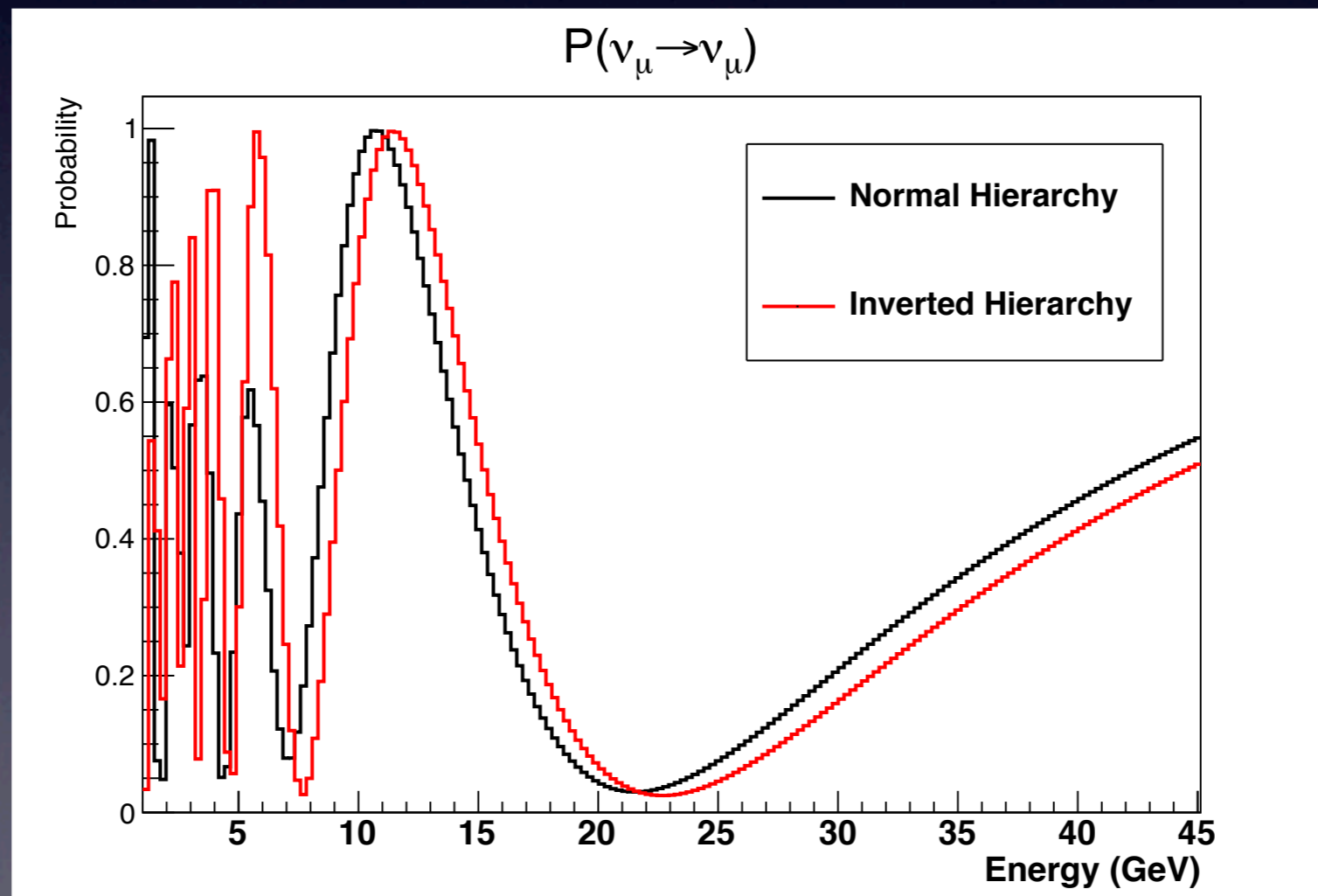
# Starting Point Math

- Interested primarily the  $\nu_\mu$  survival probability
- Note in particular the dependence on  $\Delta m^2_{31}$

$$P_{\nu_\mu \rightarrow \nu_\mu} = 1 - \cos^2 \theta_{13}^m \sin^2 2\theta_{23} \times \sin^2 \left[ 1.27 \left( \frac{\Delta m^2_{31} + A + (\Delta m^2_{31})^m}{2} \right) \frac{L}{E} \right] - \sin^2 \theta_{13}^m \sin^2 2\theta_{23} \times \sin^2 \left[ 1.27 \left( \frac{\Delta m^2_{31} + A - (\Delta m^2_{31})^m}{2} \right) \frac{L}{E} \right] - \sin^4 \theta_{23} \sin^2 2\theta_{13}^m \sin^2 \left[ 1.27 (\Delta m^2_{31})^m \frac{L}{E} \right]$$

# Starting Point Plots

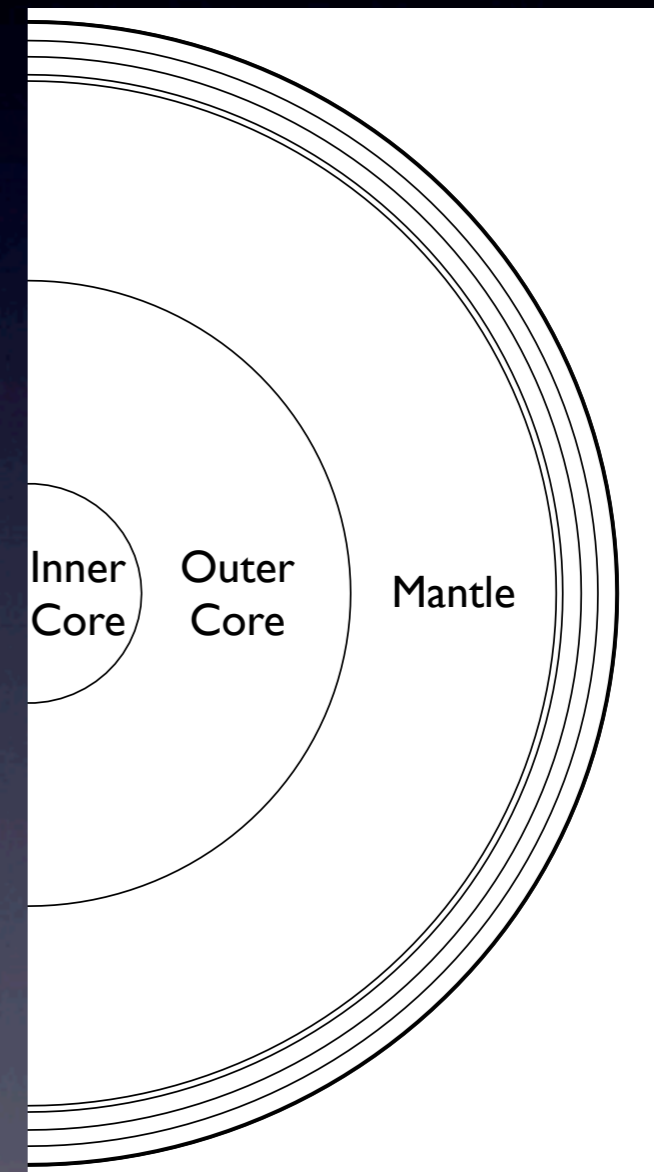
- Clear differences emerge between the hierarchies
- This is at a fixed zenith angle,  $\sim 150$  degrees





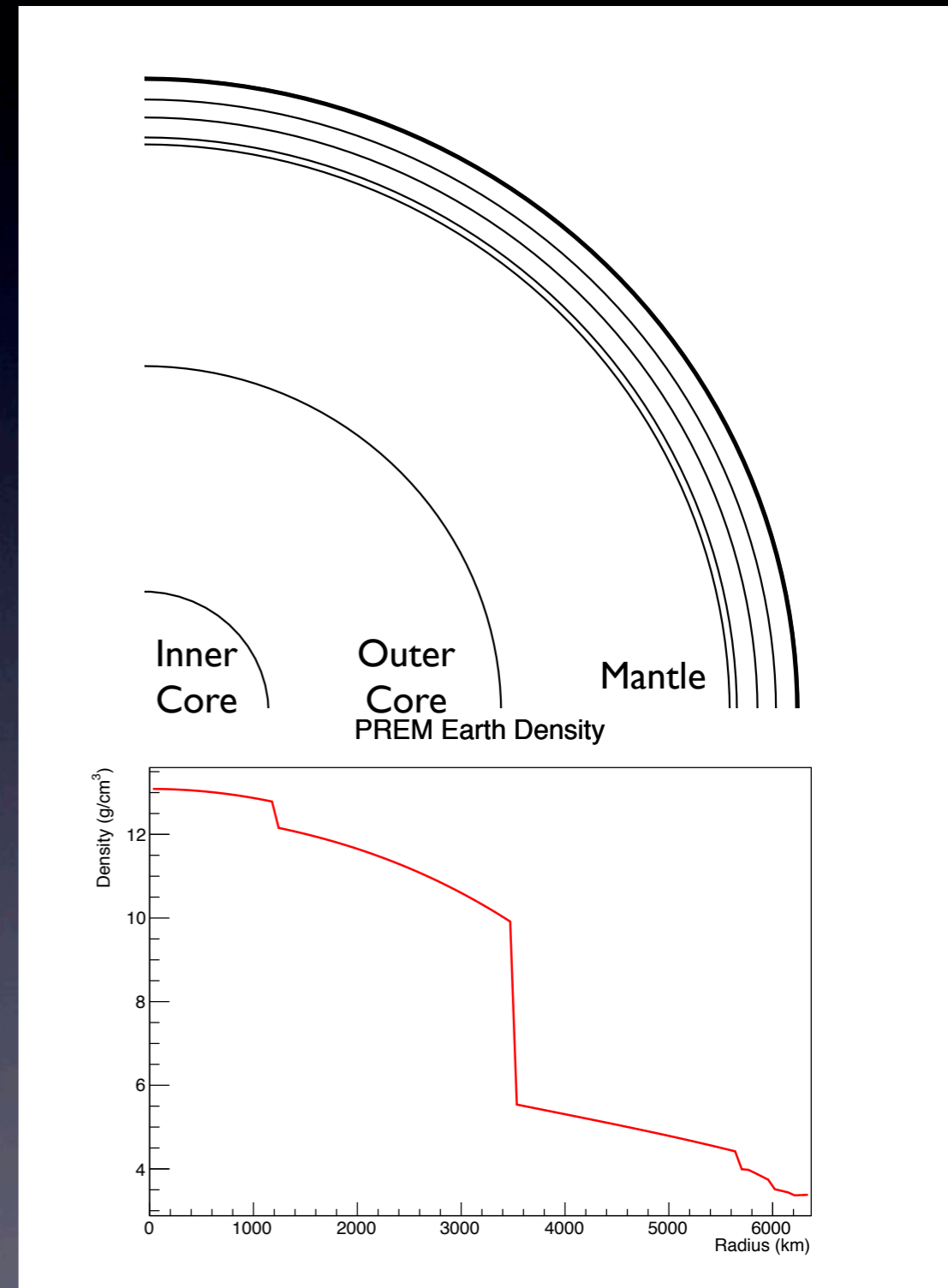
# Preliminary Reference Earth Model (PREM)

- Current “best guess” as to the variation of density in the Earth
- Been around a long time, still retains the preliminary name



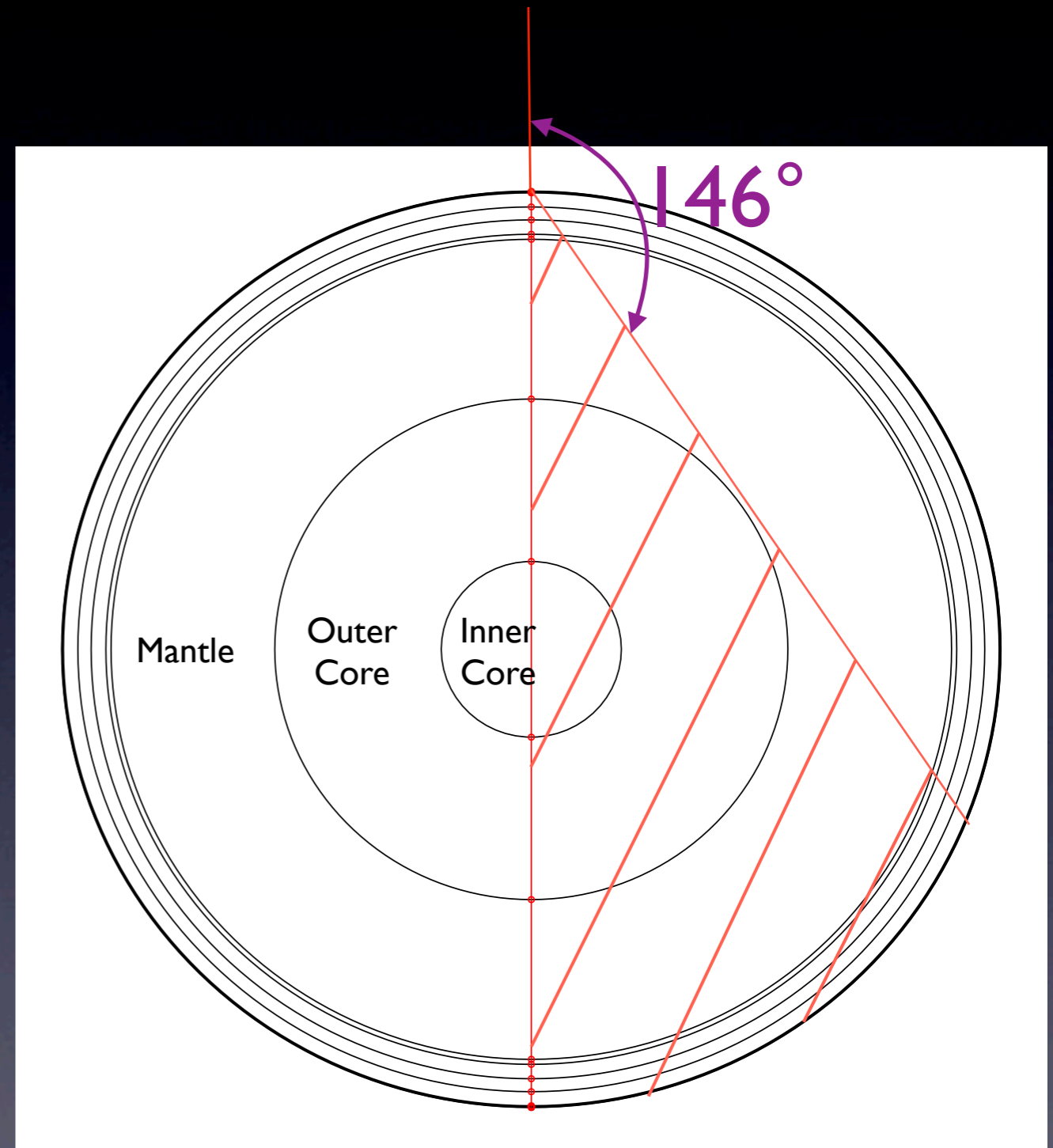
# Matter effects

- Previous probabilities were just for one path length
- upgoing neutrinos experience effect of traveling through the Earth (or a fraction of it)



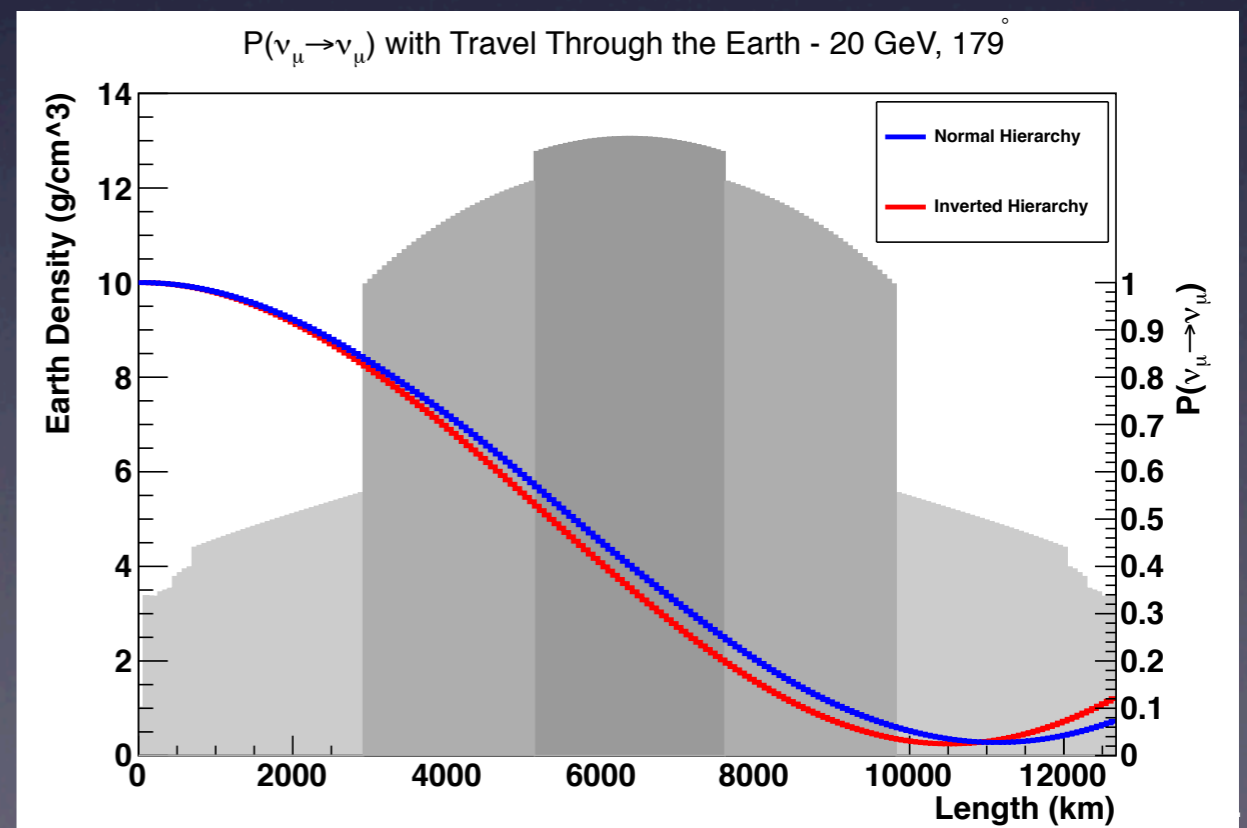
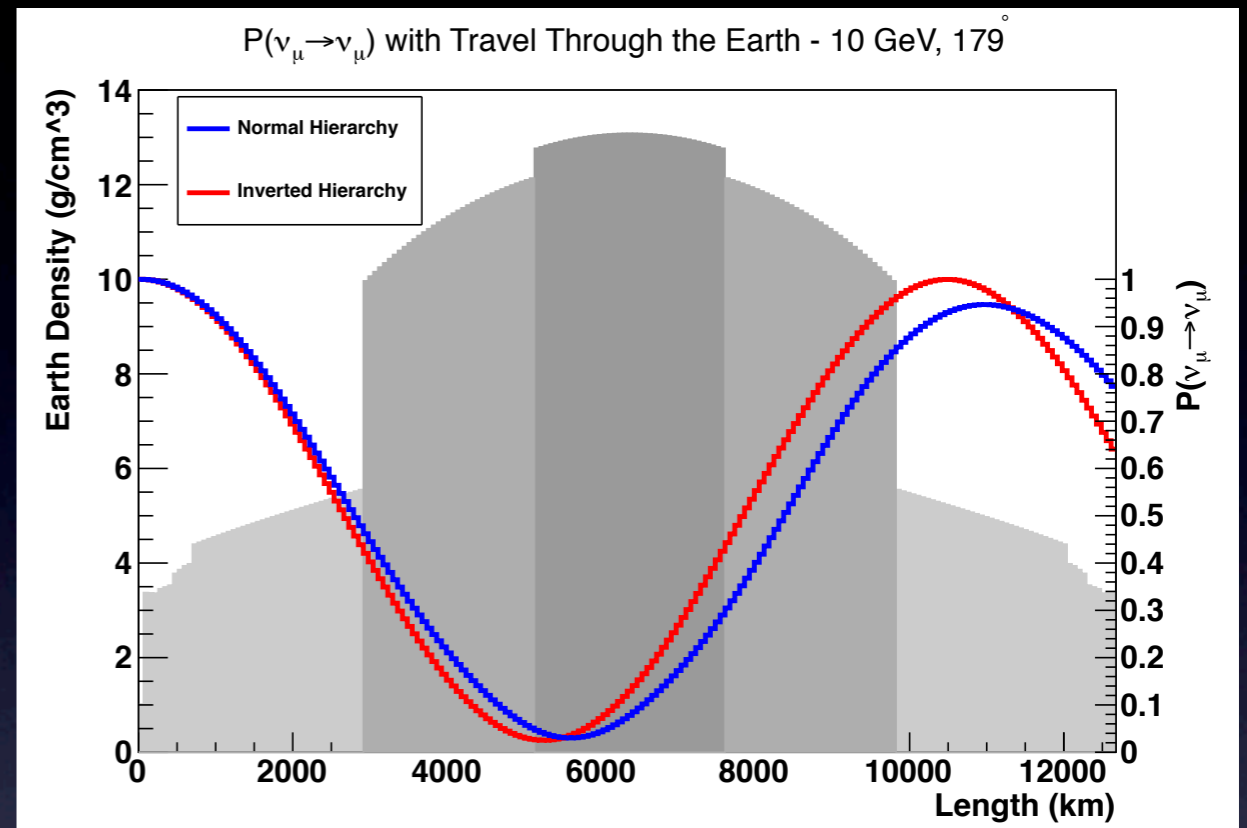
# Matter Effects - I

- At angles  $> 146^\circ$
- $\nu$  pass through mantle and core
- parametric enhancement of oscillations take place



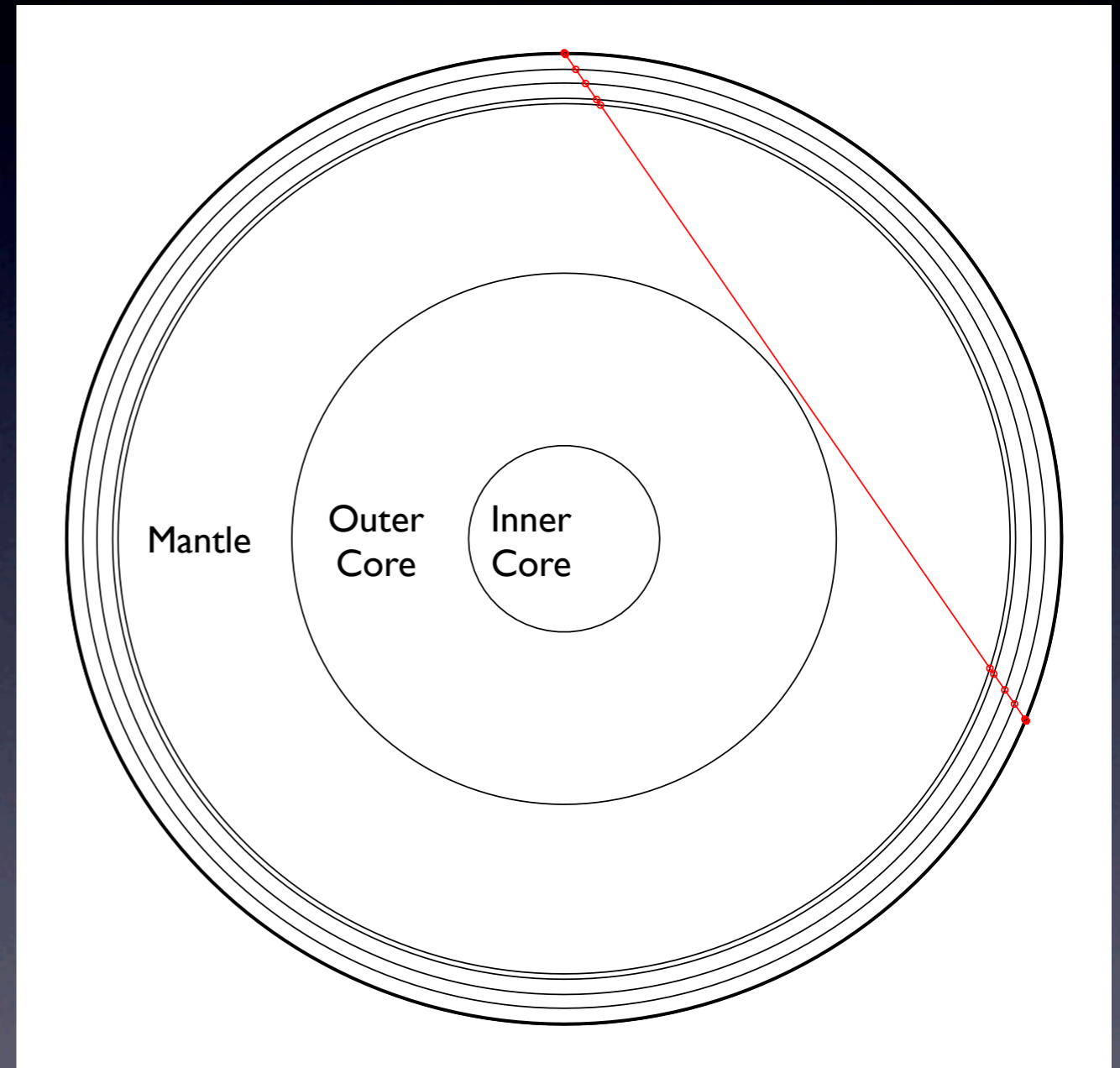
# Matter Effects

- These are almost directly upgoing
- Two different energies show magnitude of final effect
- This zenith dominated by parametric resonance



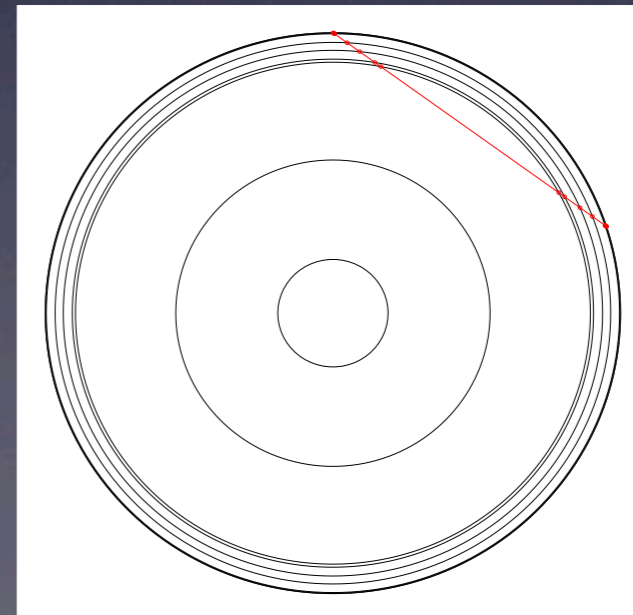
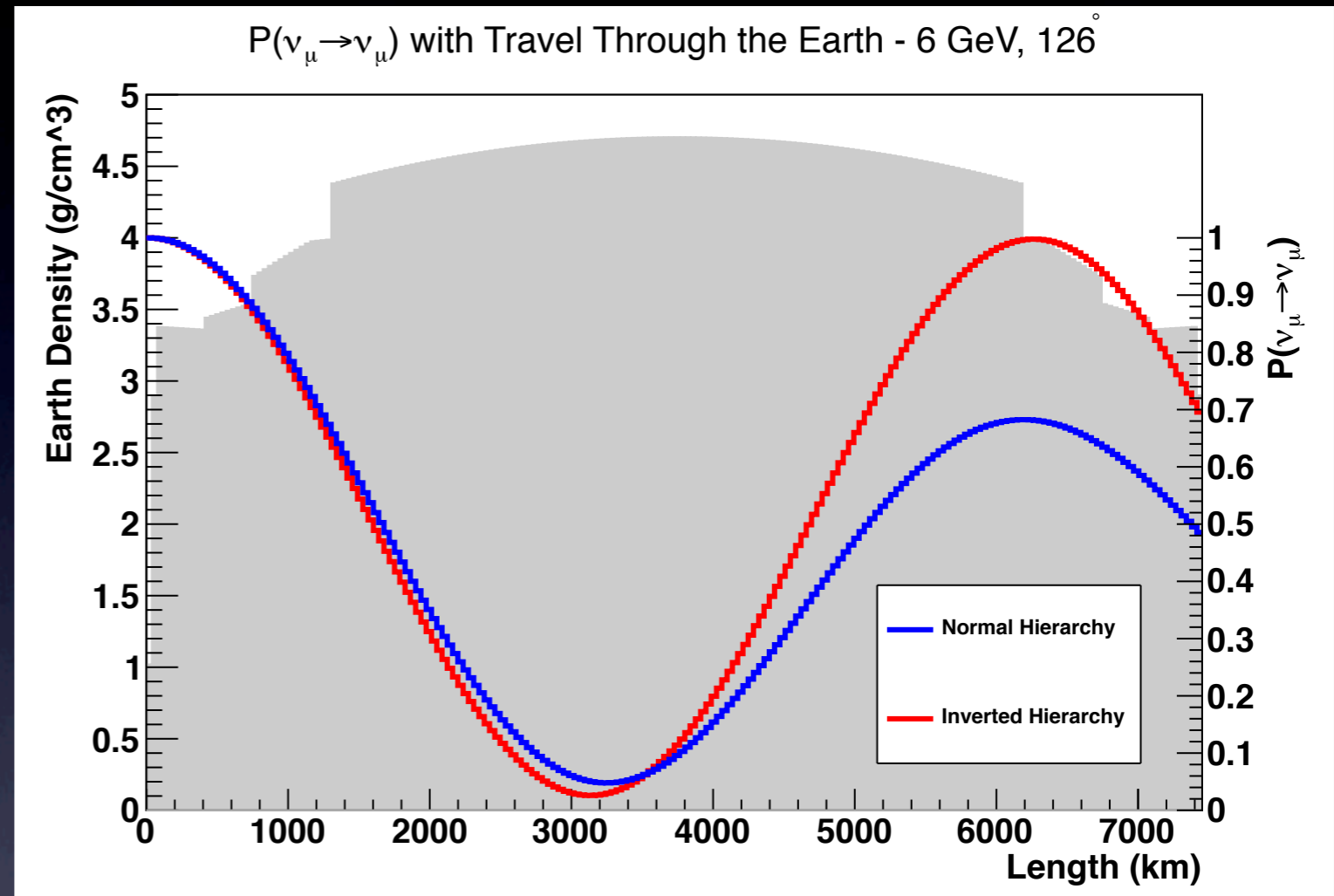
# Matter Effects - II

- At angles  $< 146^\circ$ 
  - $\nu$  pass through mantle only
- MSW enhances  $\nu_\mu$  to  $\nu_e$



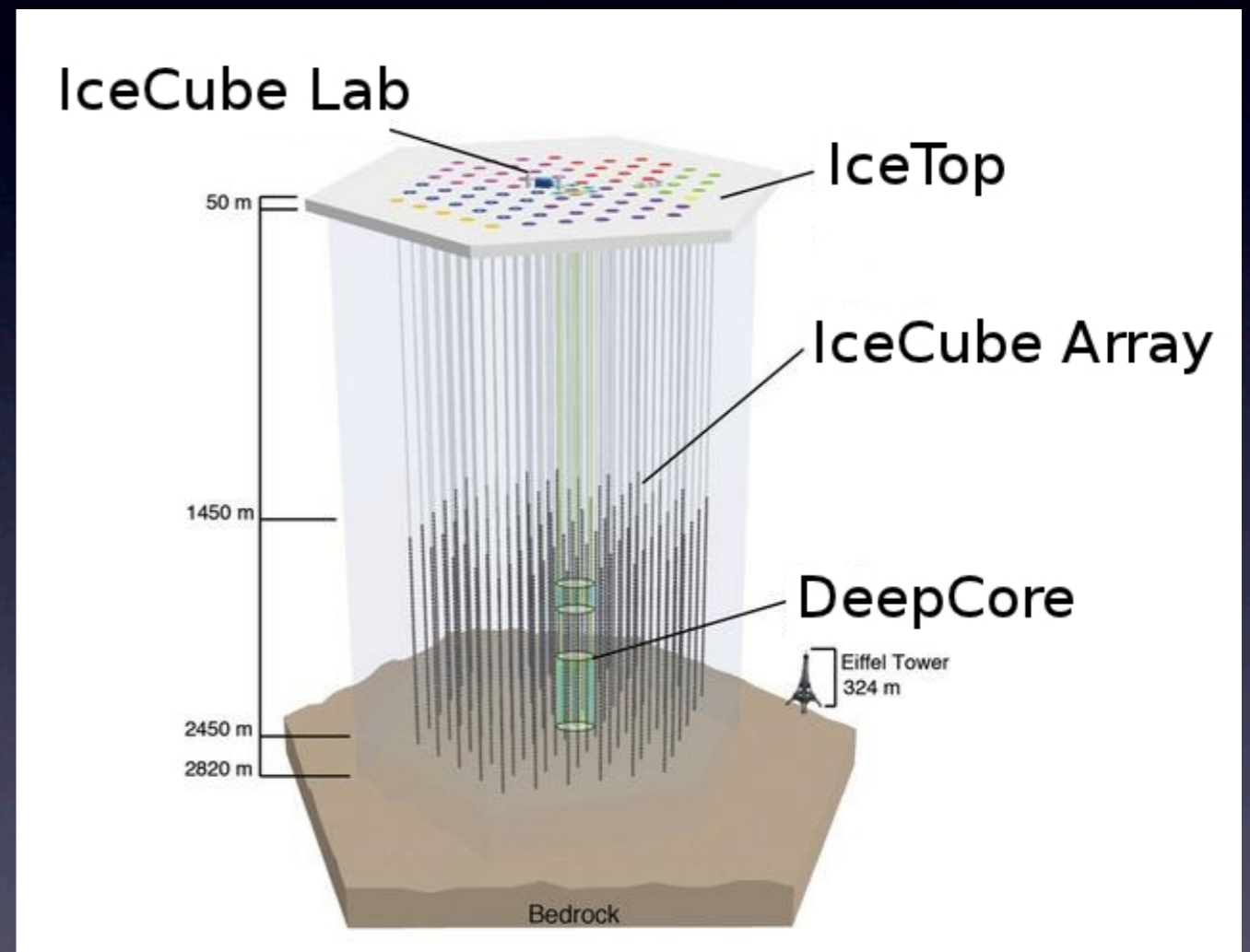
# Matter Effects

- Much less upgoing angles show MSW effects
- Note change in Earth density plot



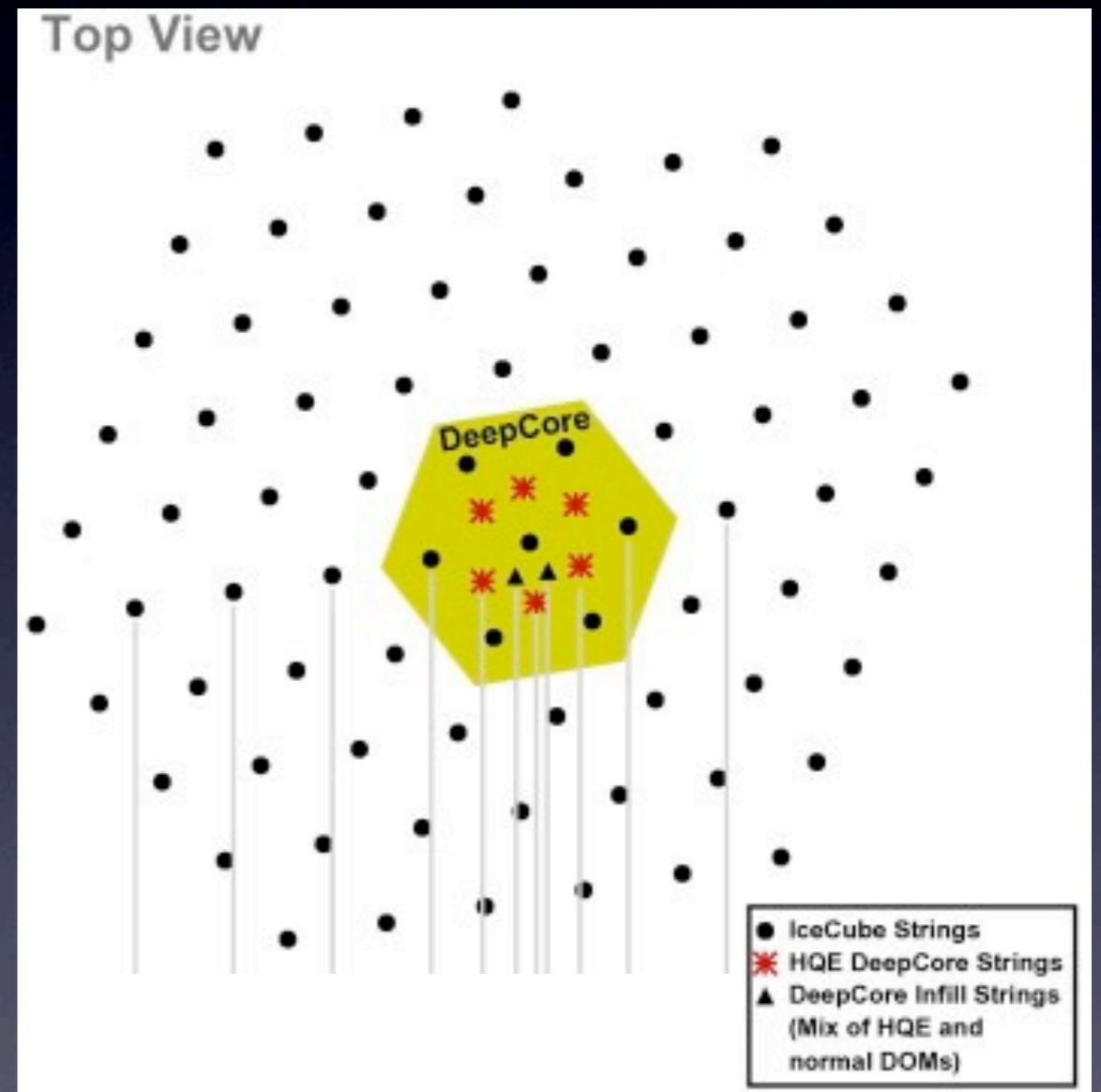
# Detection Method

- IceCube and DeepCore successfully detecting neutrinos for years
- IceCube: ~5160 PMTs in  $1 \text{ km}^3$
- DeepCore: denser string and DOM spacing
- High efficiency PMTs



# Detection Method

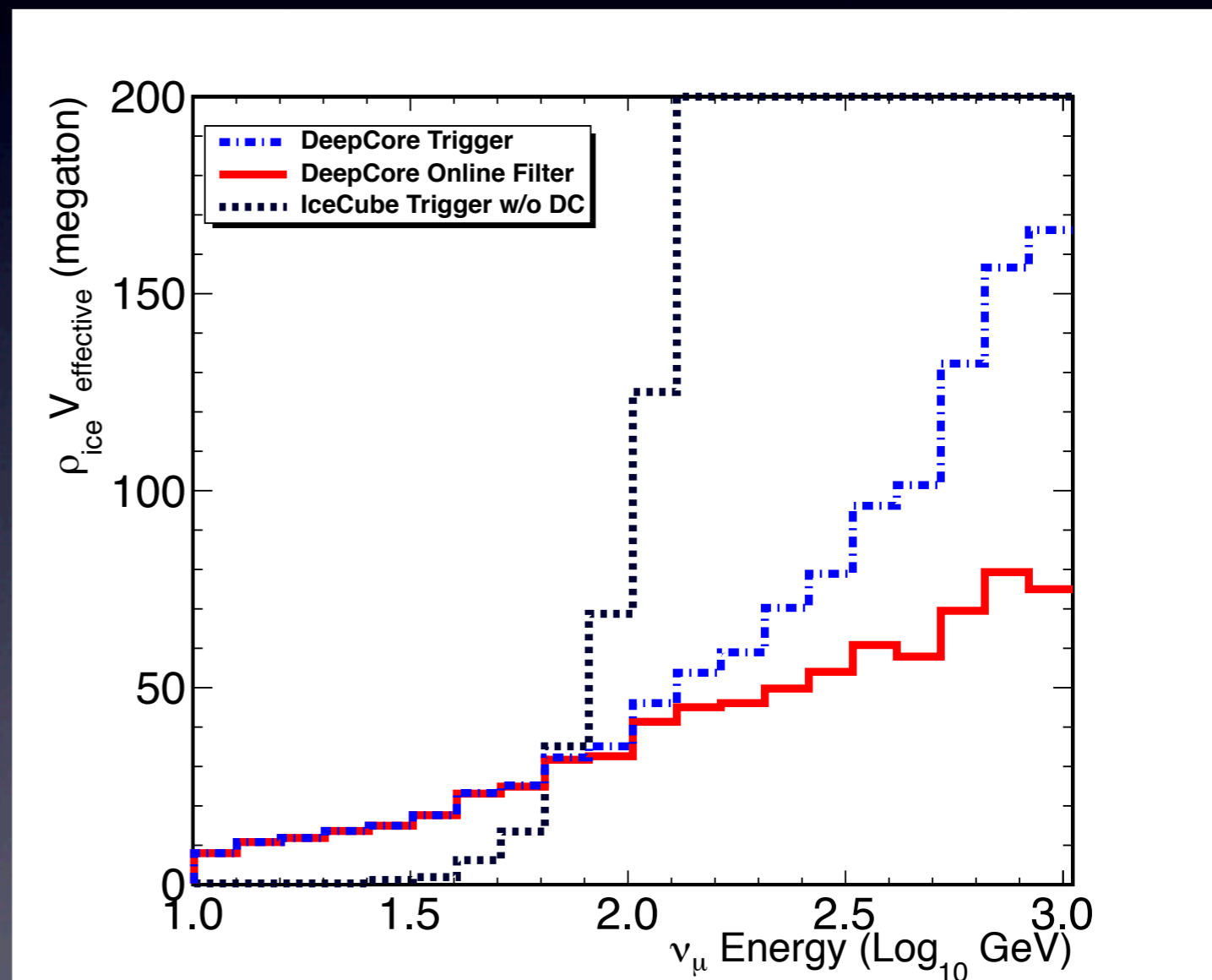
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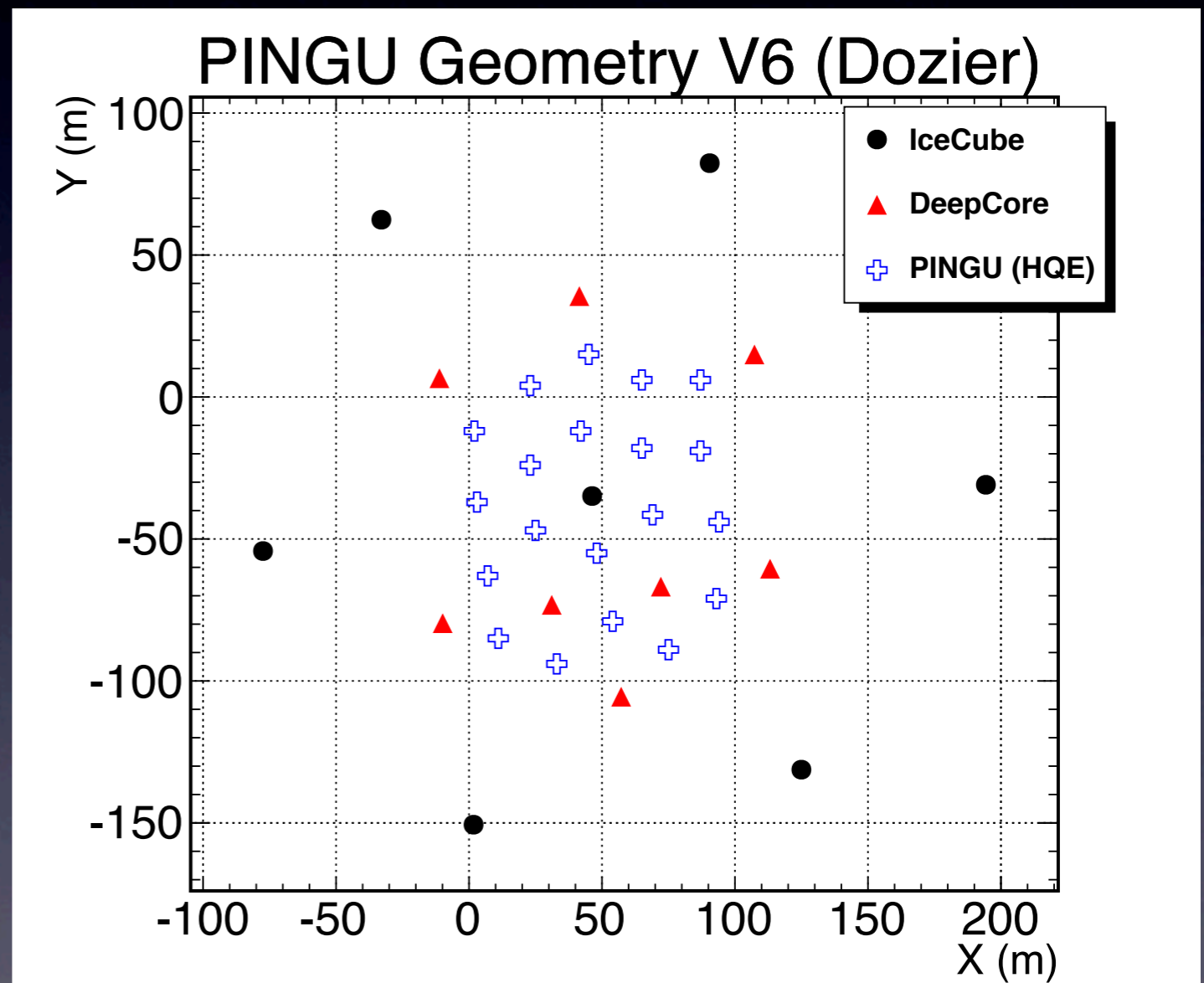
# DeepCore Energy Range

- Detection threshold lowered to  $\sim 10$  GeV in DeepCore
- Effective volume at trigger level increased below 100 GeV



# Step up to PINGU

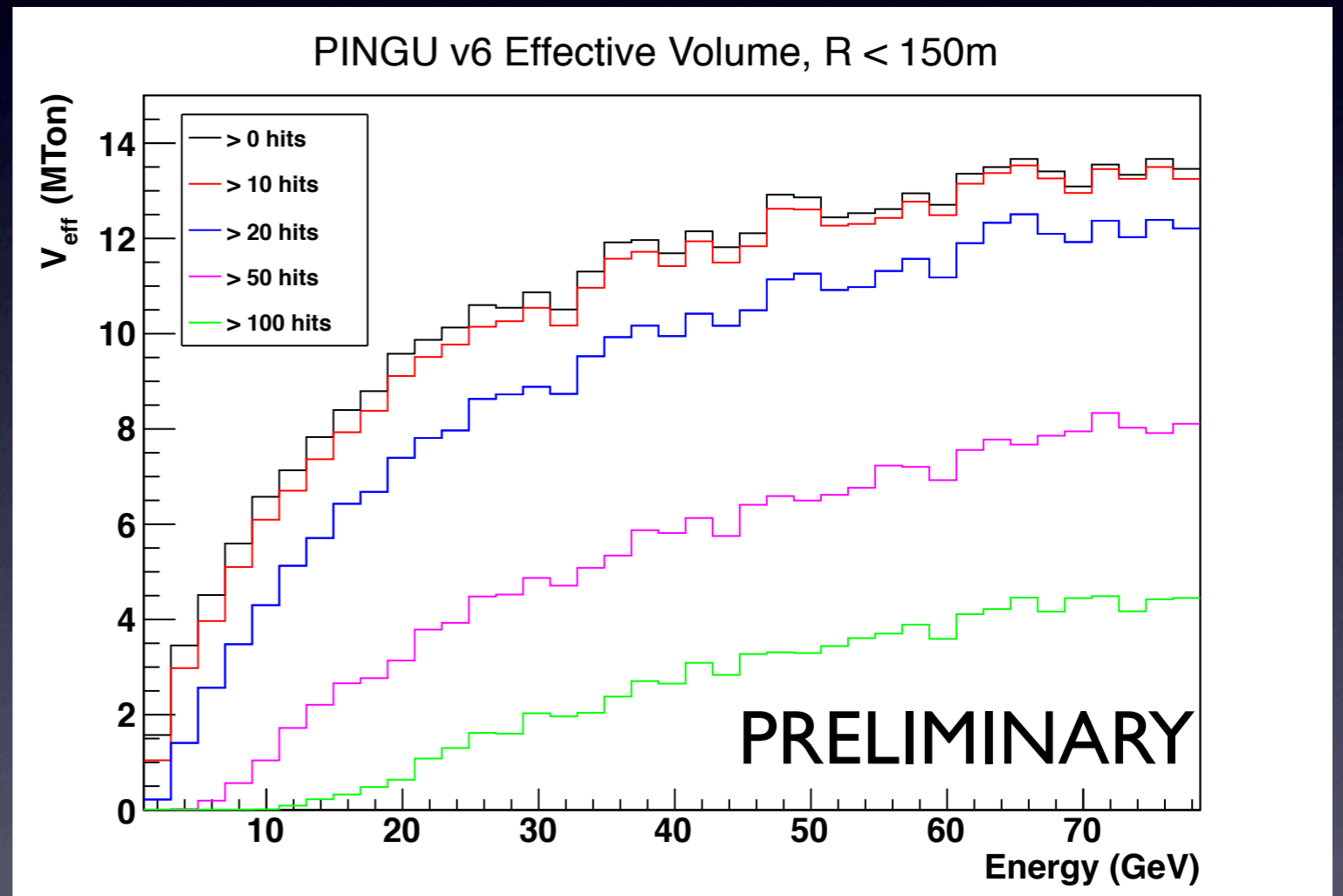
- Add another 20 strings
- Denser string and DOM spacing
- Energy threshold lowers again



# Step up to PINGU

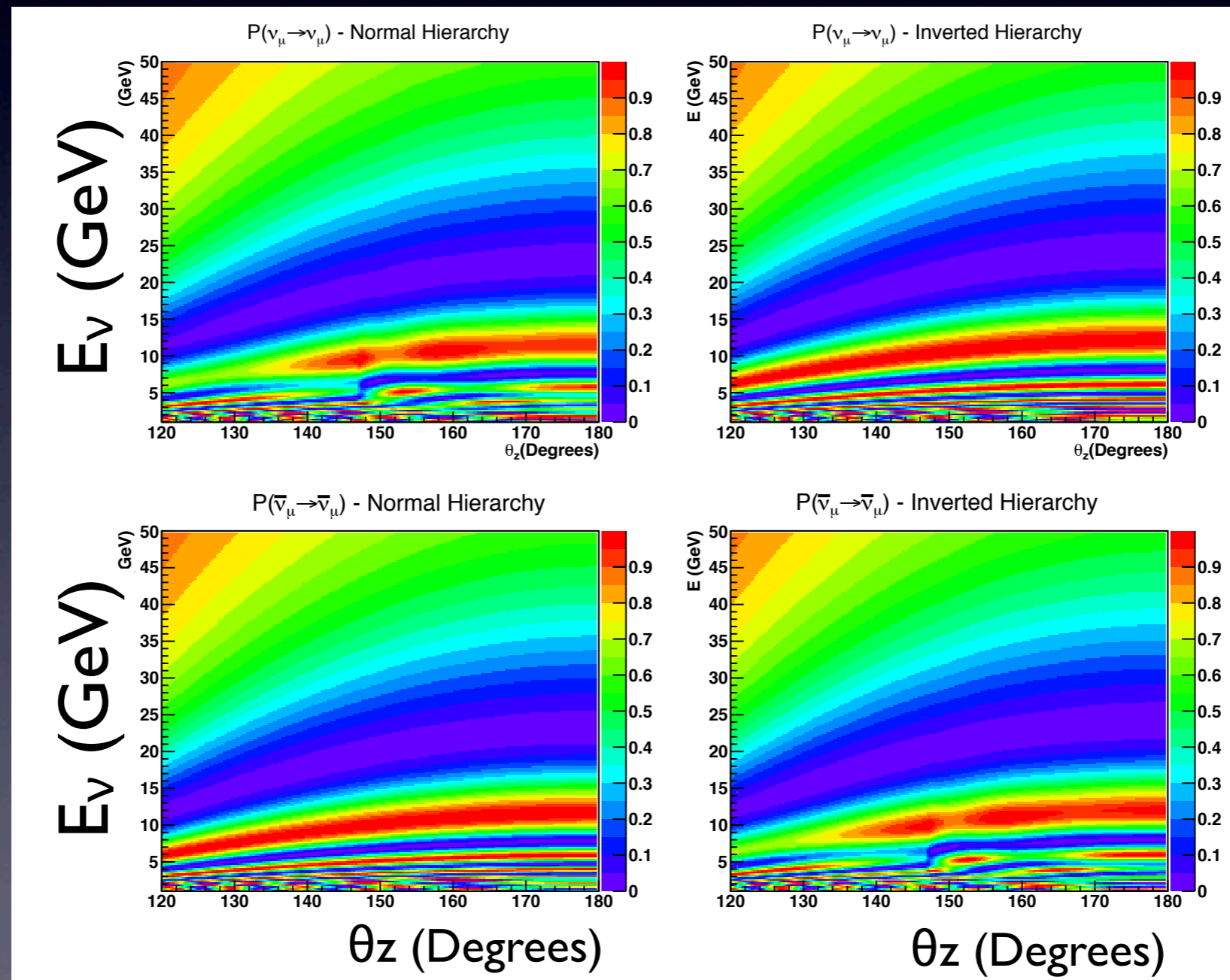
PRELIMINARY

- Add another 20 strings
- Denser string and DOM spacing
- Energy threshold lowers again



# 2 Dimensional Plotting

- Now we need to extend this to two dimensions to show the probability vs energy and zenith angle



# Distinguishability

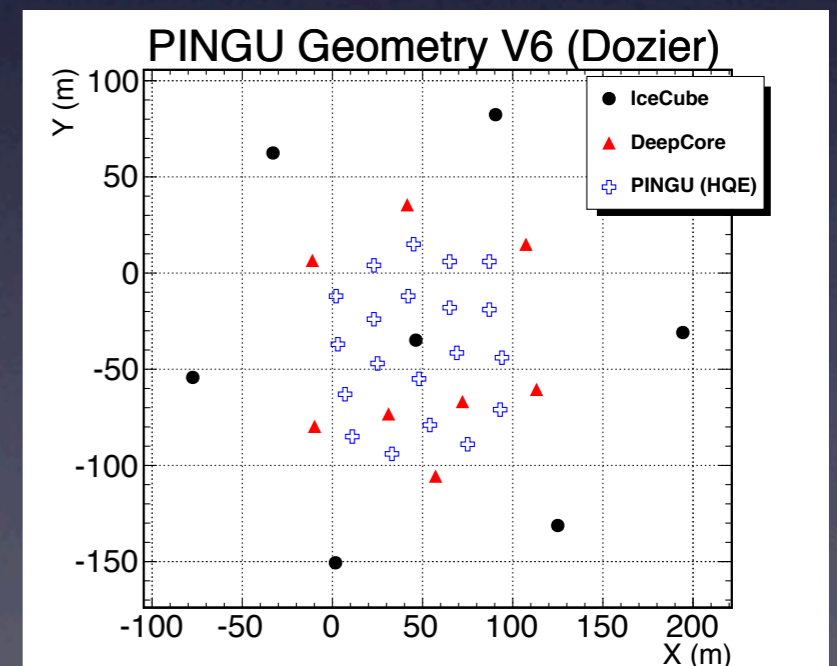
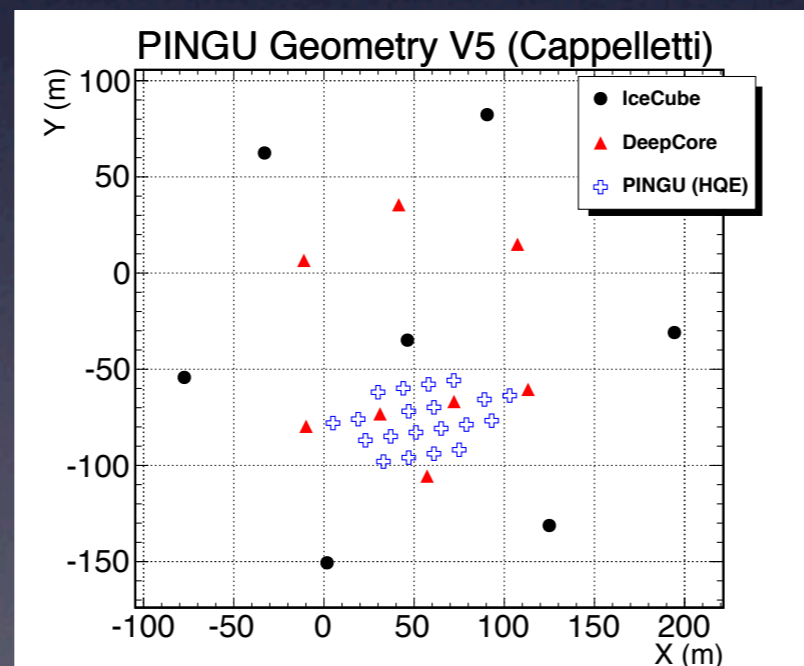
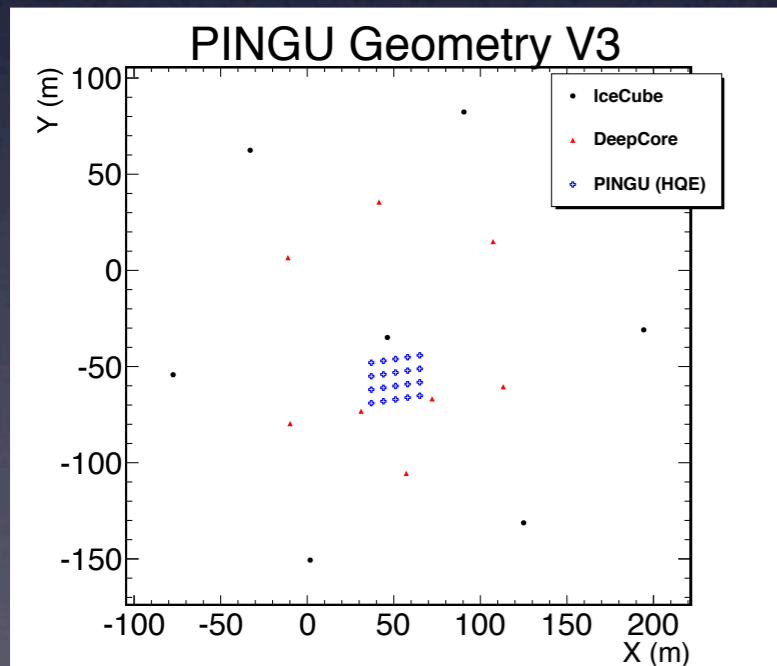
- Use method outlined in arXiv:1205.7071 (Akhmedov, Razzaque and Smirnov)

$$S^{tot} = \sqrt{\sum_{ij} \frac{(N_{ij}^{IH} - N_{ij}^{NH})^2}{N_{ij}^{NH}}}$$

- Essentially bin everything up and subtract the two hierarchies, scaled by the number of events in the Normal hierarchy bin

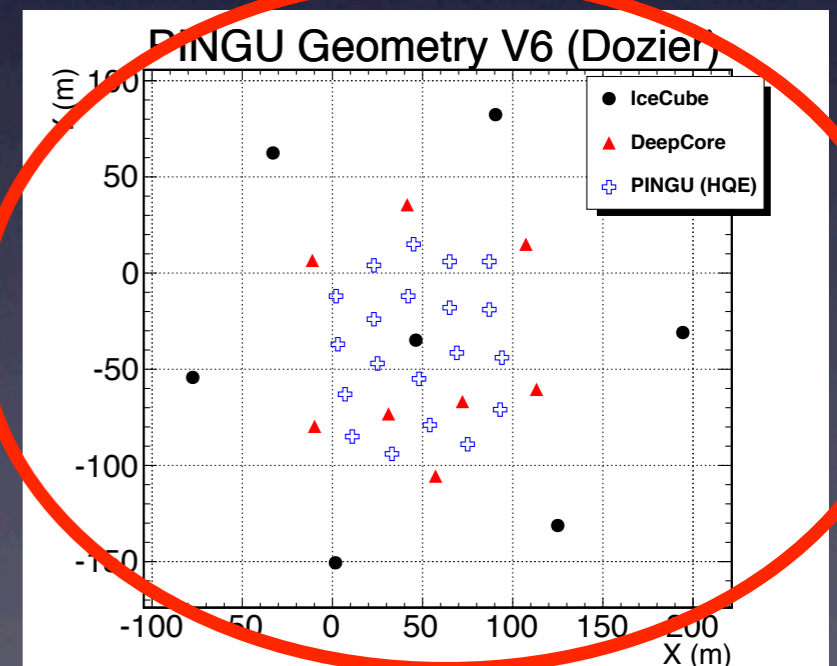
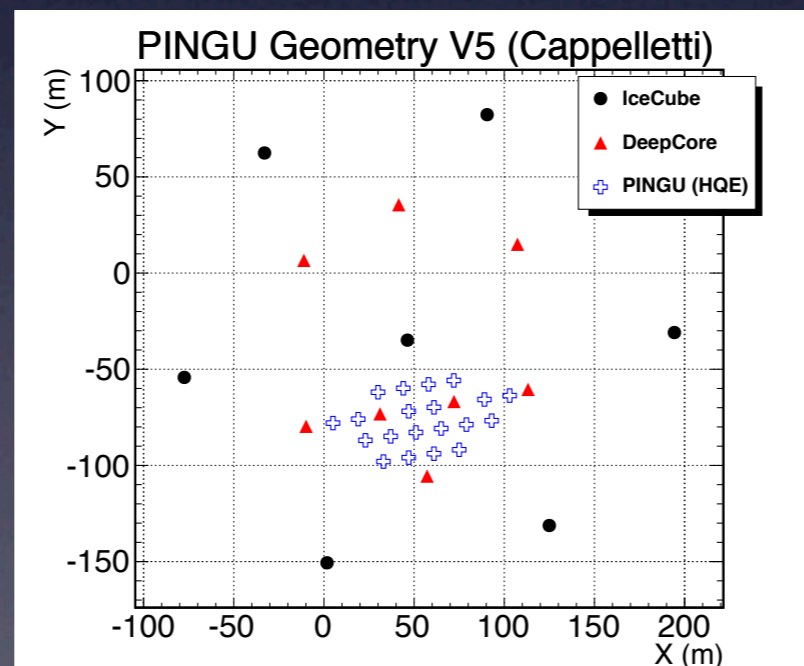
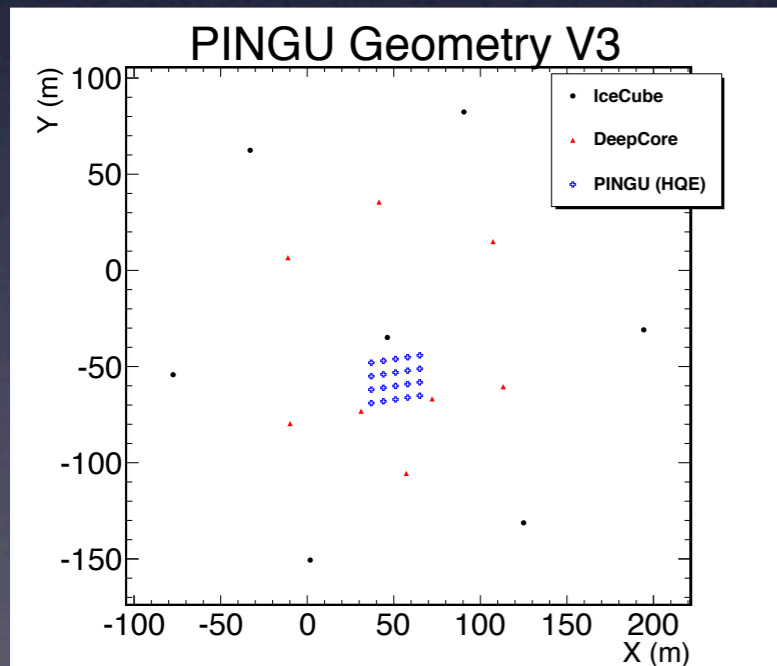
# Simulations

- Simulations now carried out using IceCube MC structure
- Currently studying different PINGU geometries with different spacings



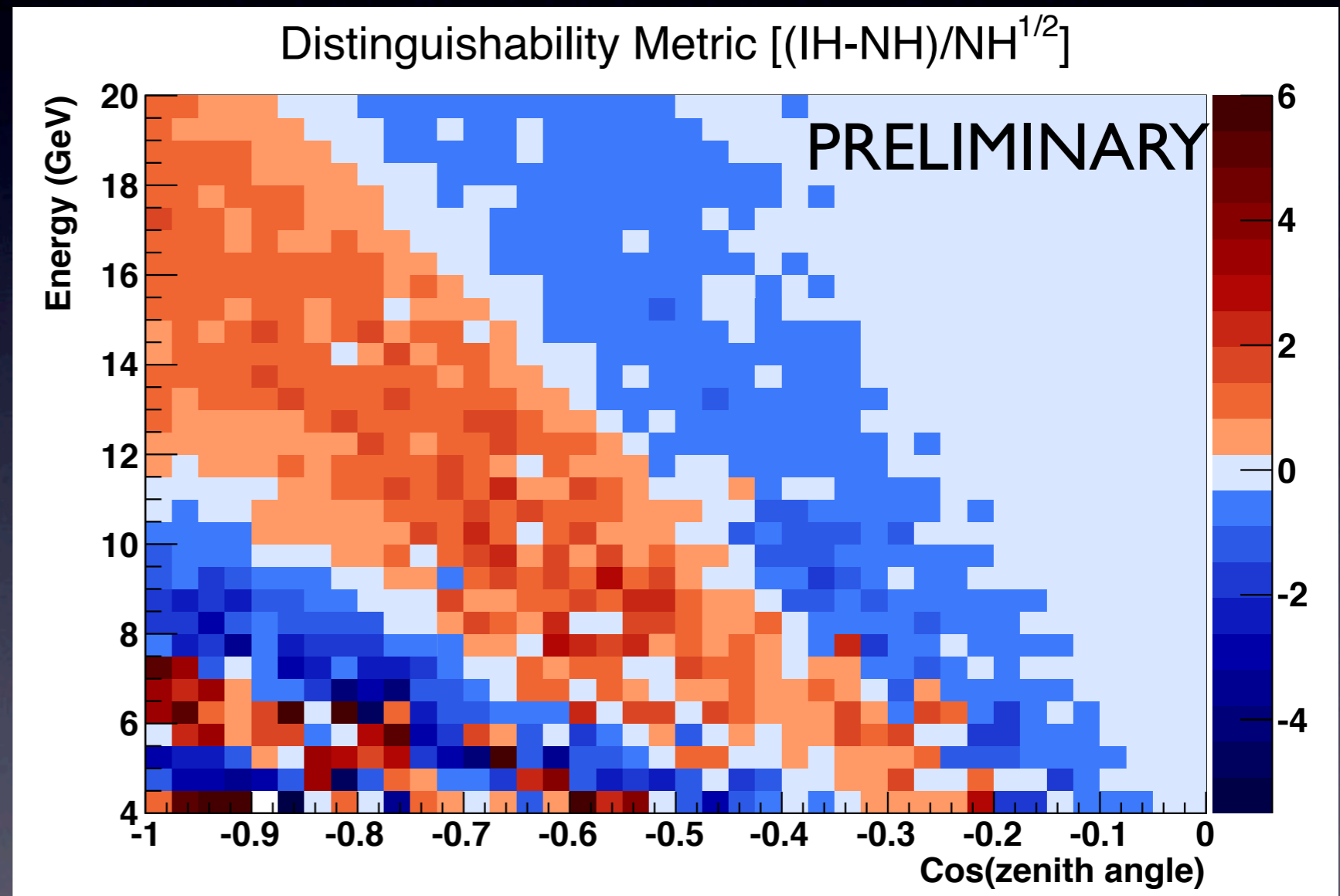
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# Distinguishability Plots

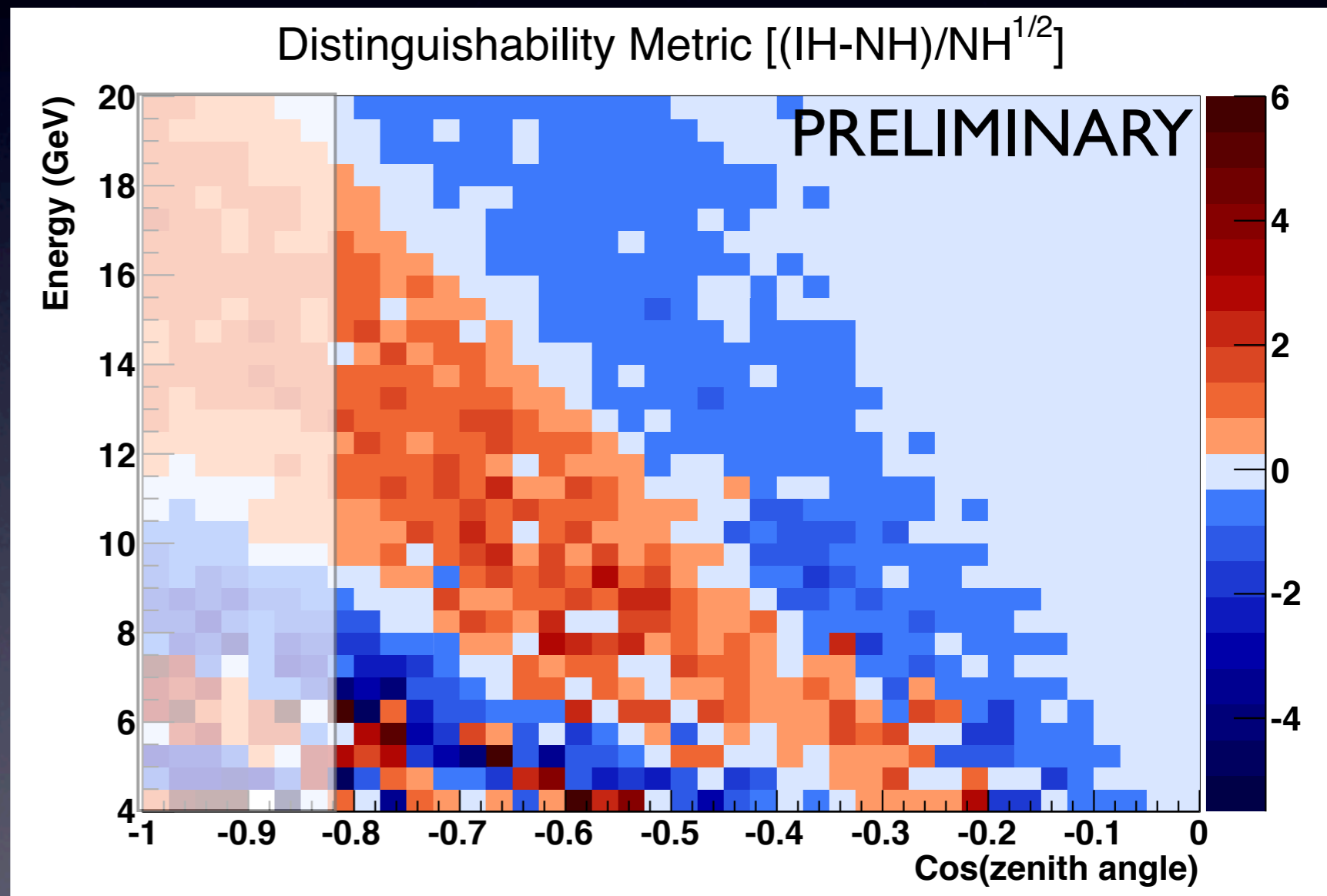
- Use our simulations
- First use neutrino zenith angle and energy
- Shown without square root to illustrate pattern





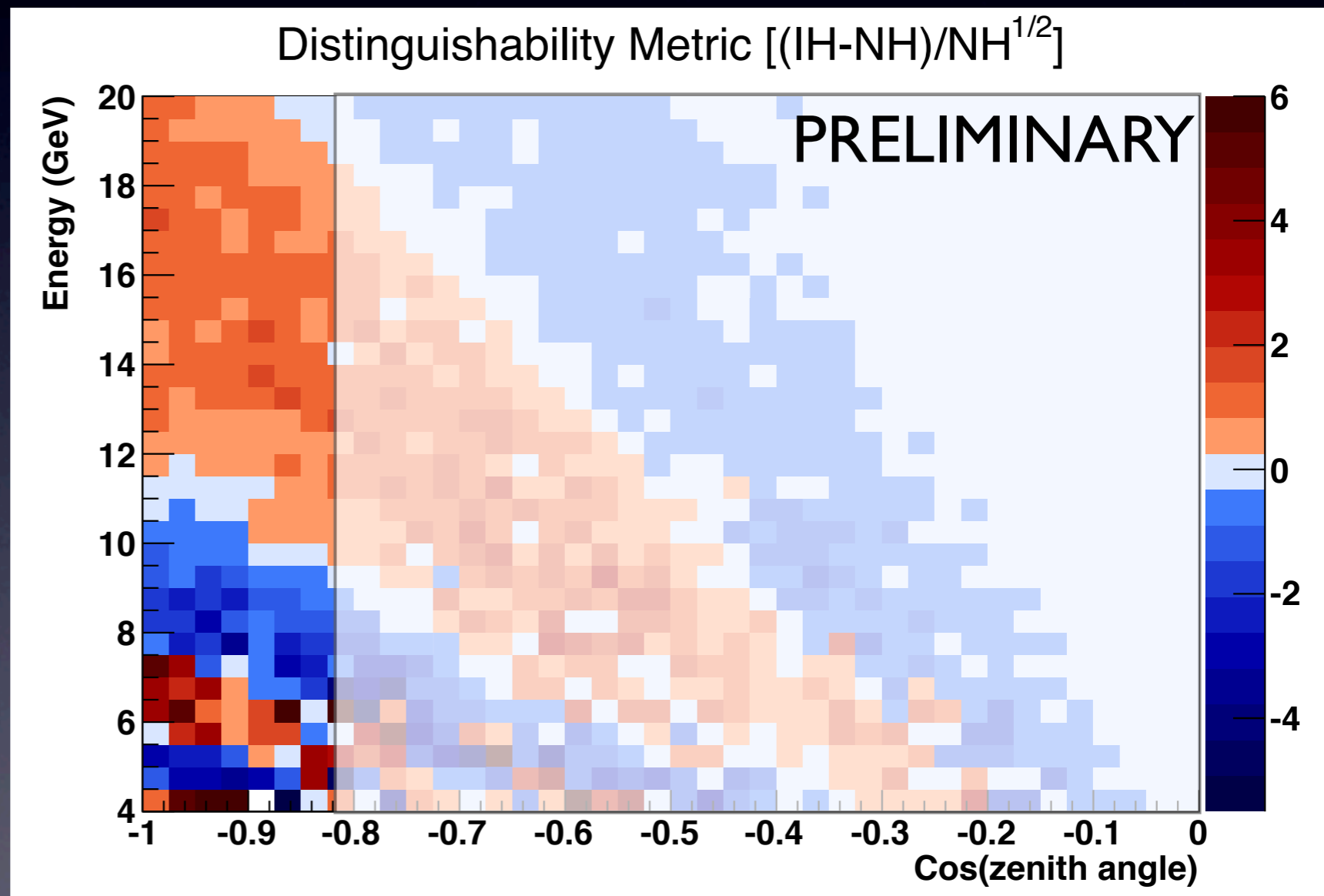
# Distinguishability Plots

- Matter effects due to MSW



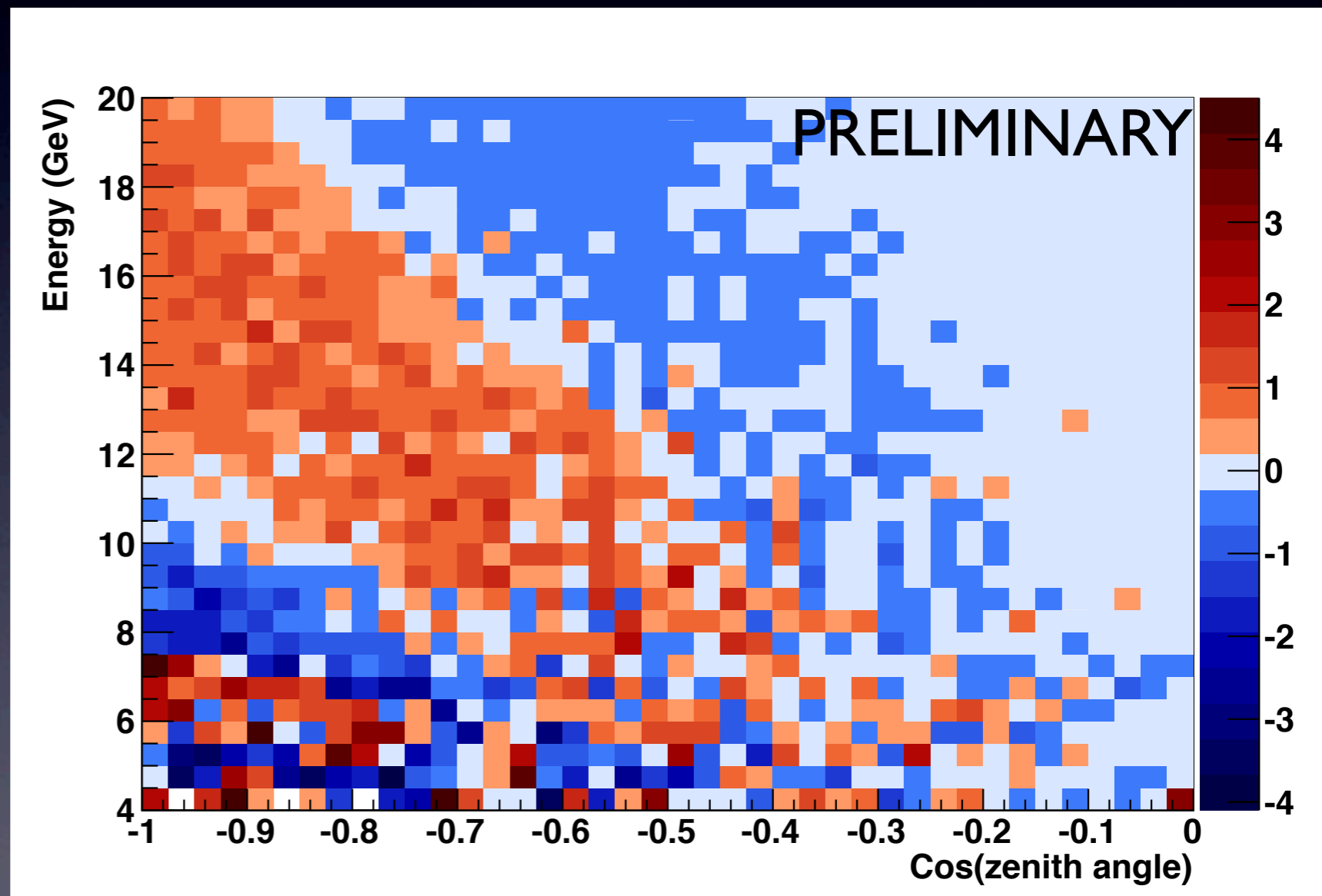
# Distinguishability Plots

- Primarily parametric oscillation effects in this region



# Distinguishability Plots

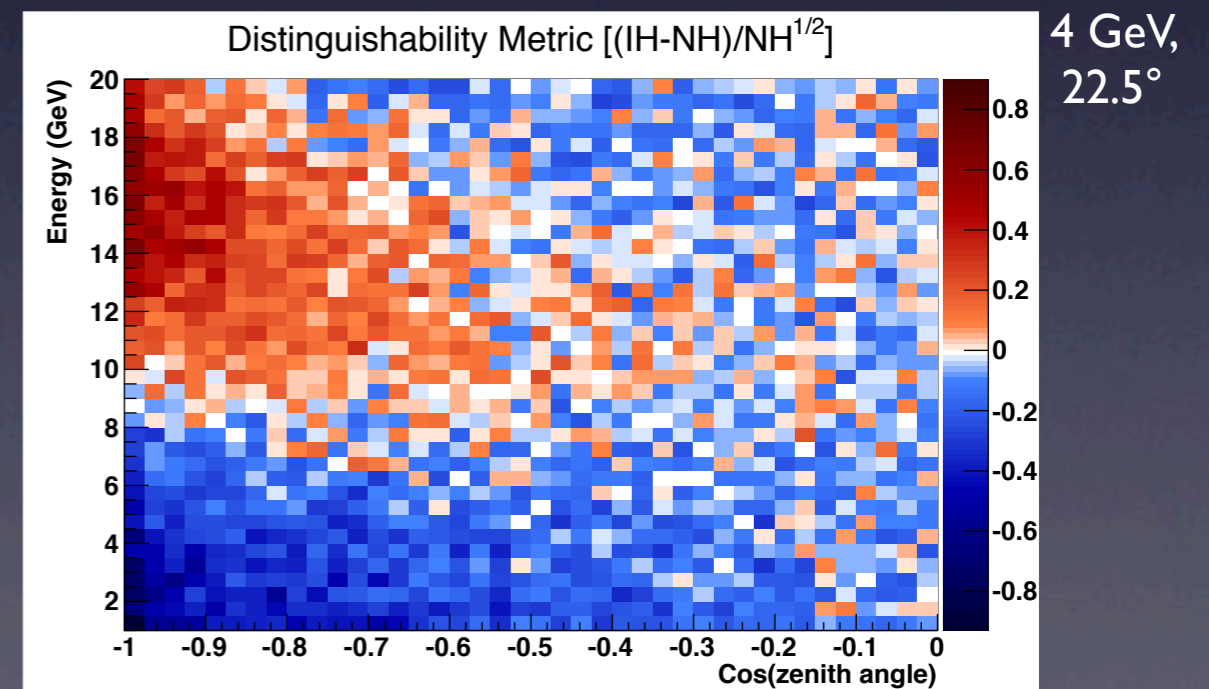
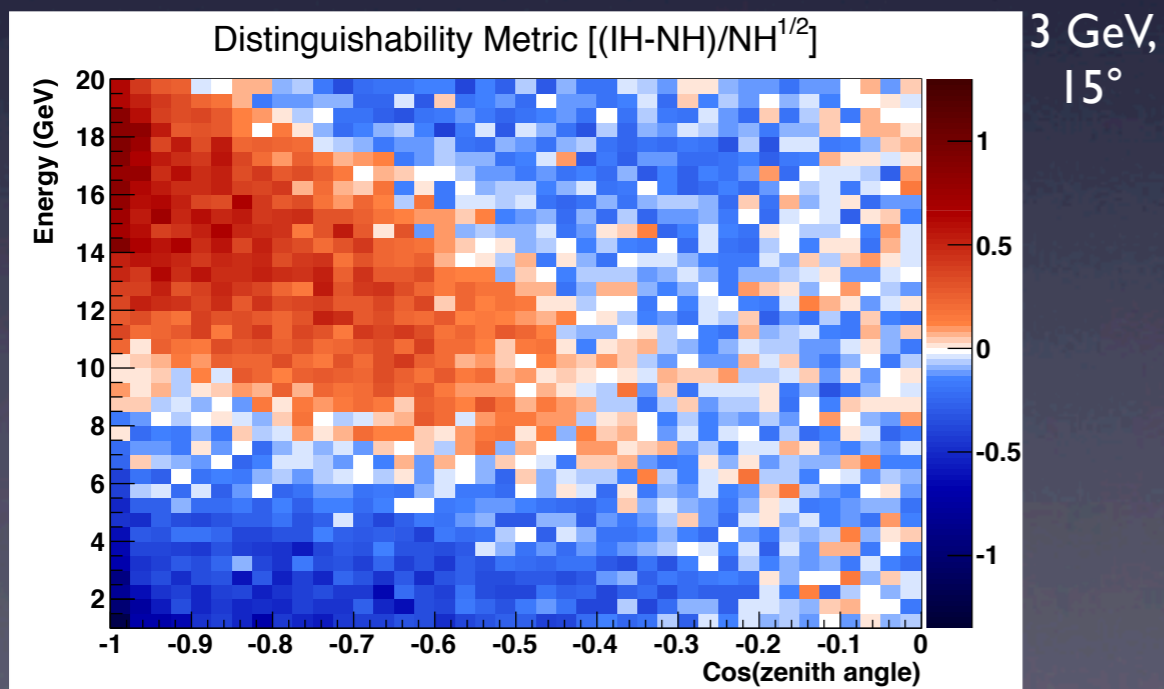
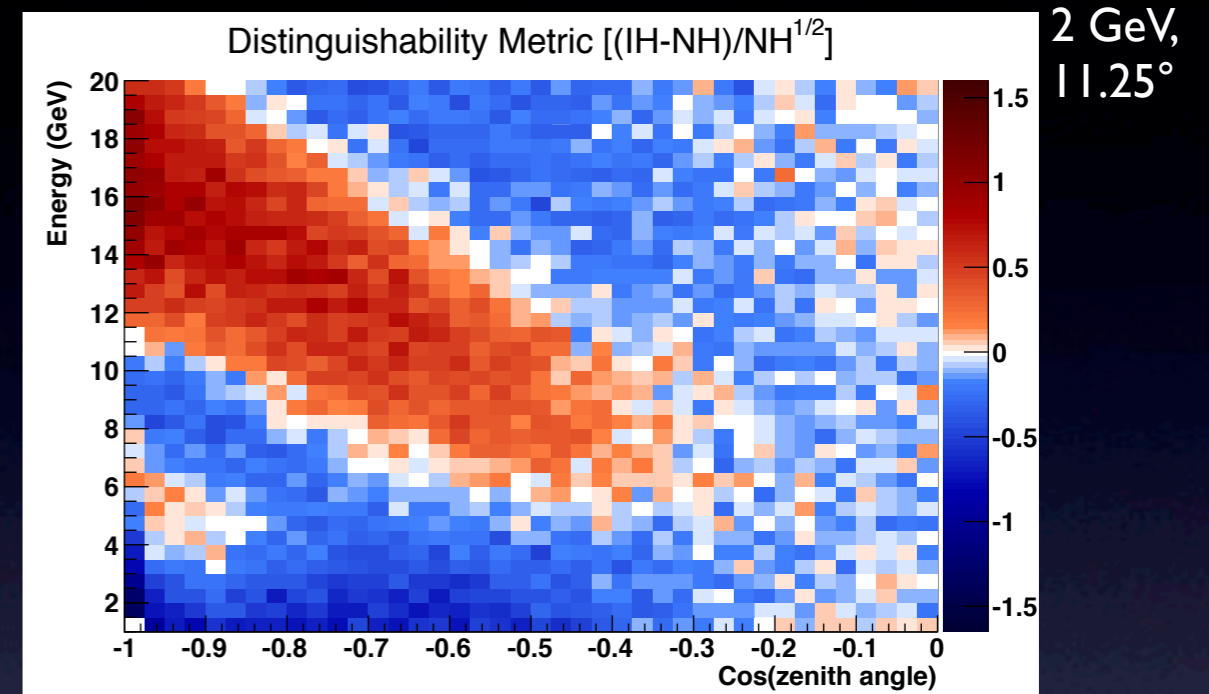
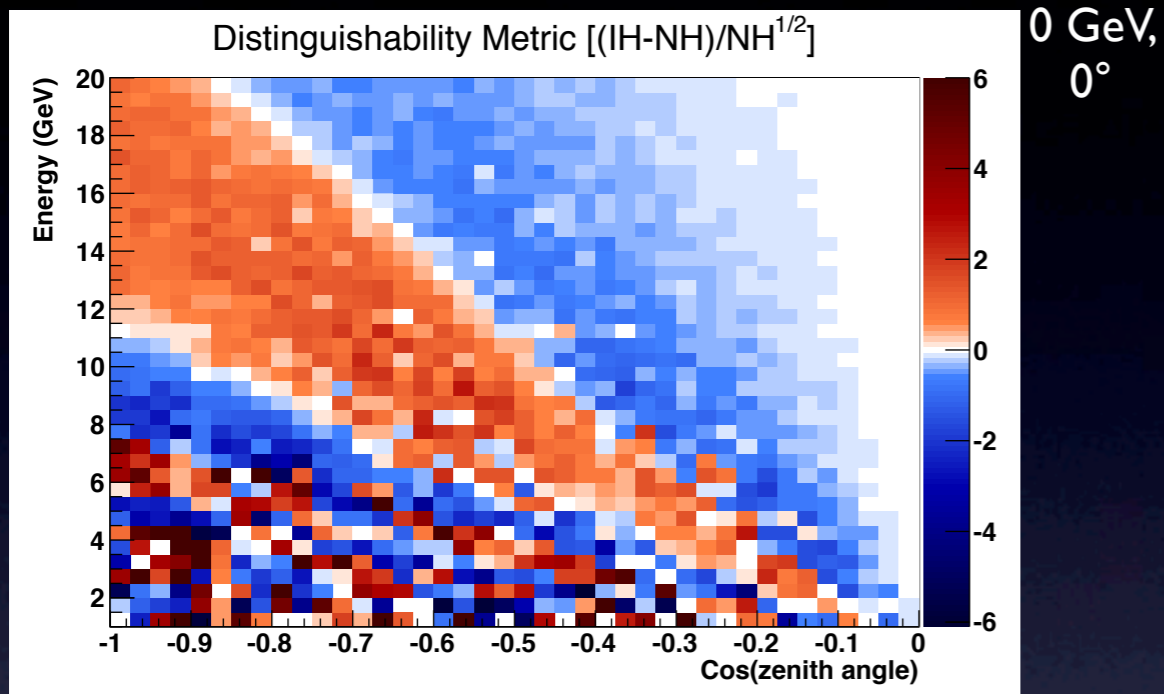
- Then use muon zenith angle and neutrino energy
- Shown without square root to illustrate pattern



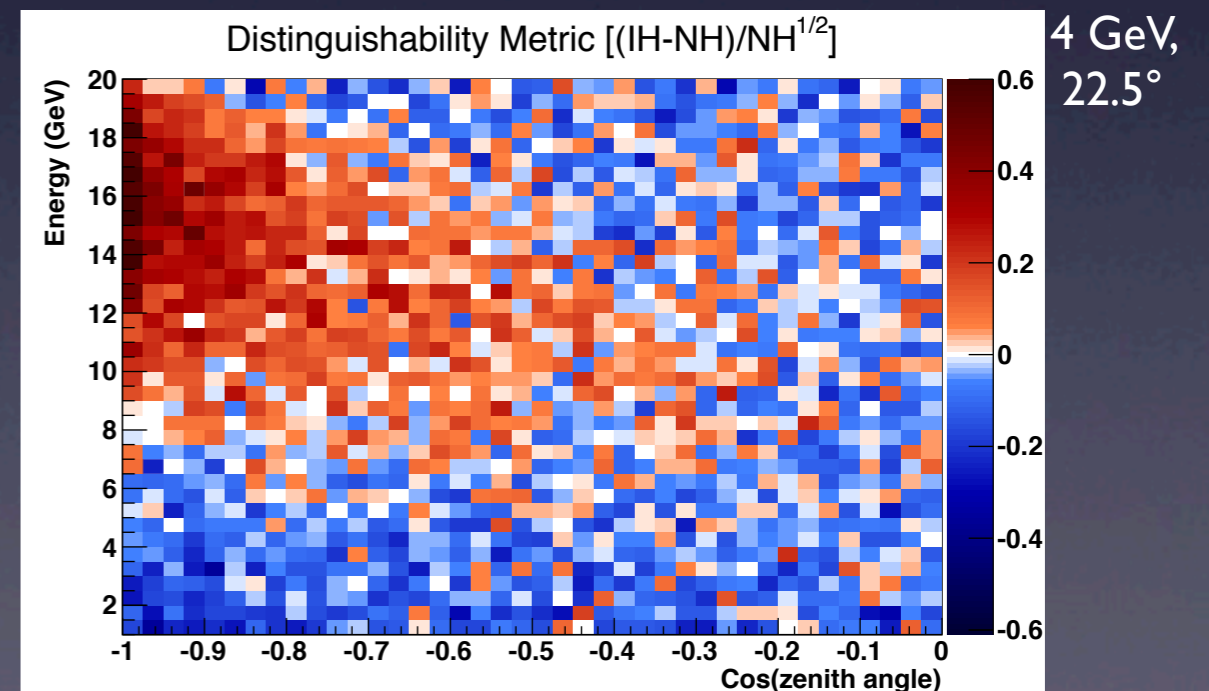
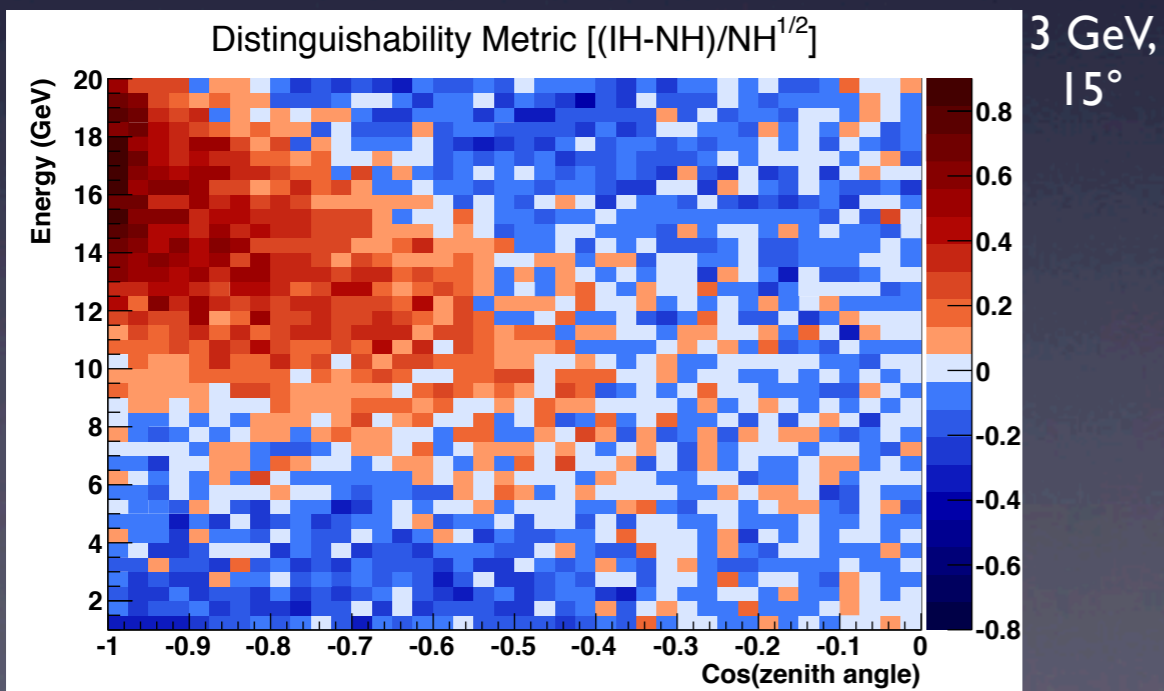
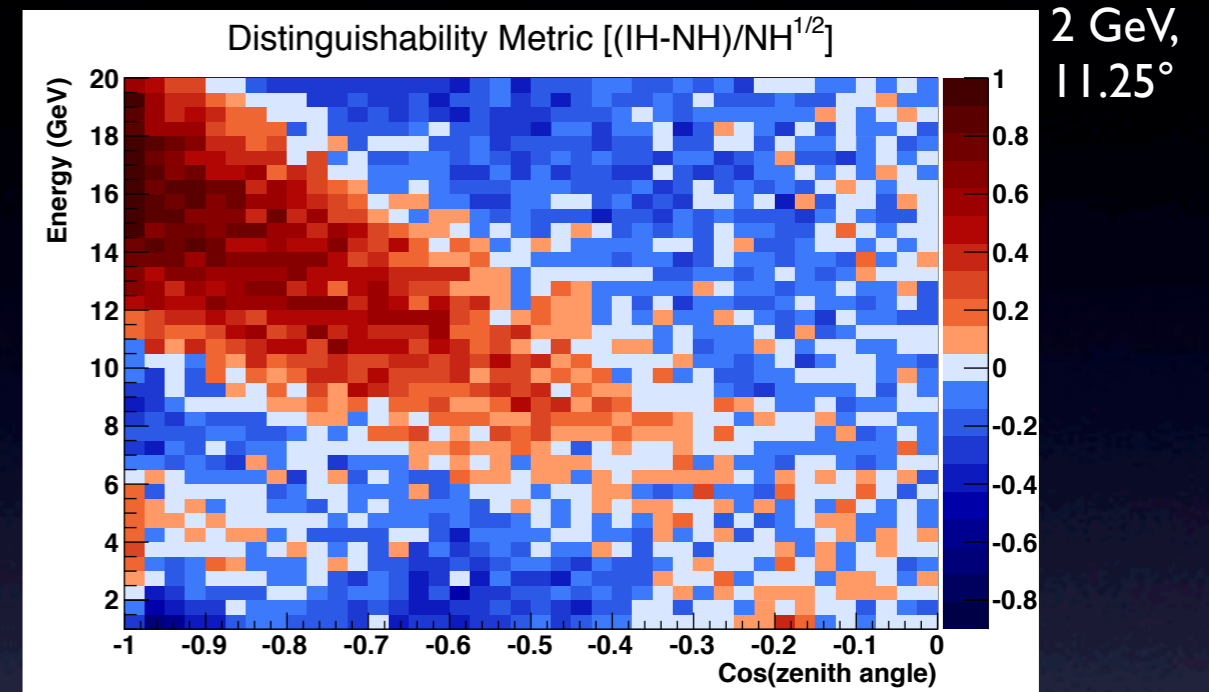
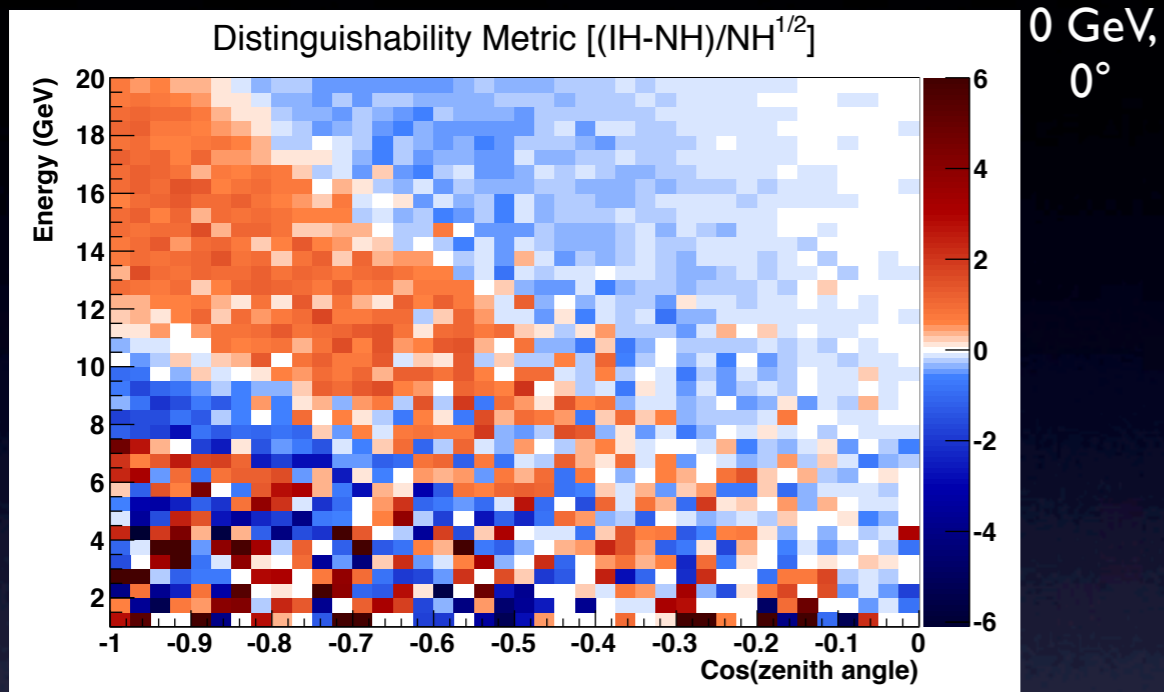
# Reconstruction

- Previous plots showed perfect detector resolution
- This (probably) won't be the case
- Need to account for the reconstruction effects
- Add a gaussian “smearing” to the angles and energies

# Detector Resolution

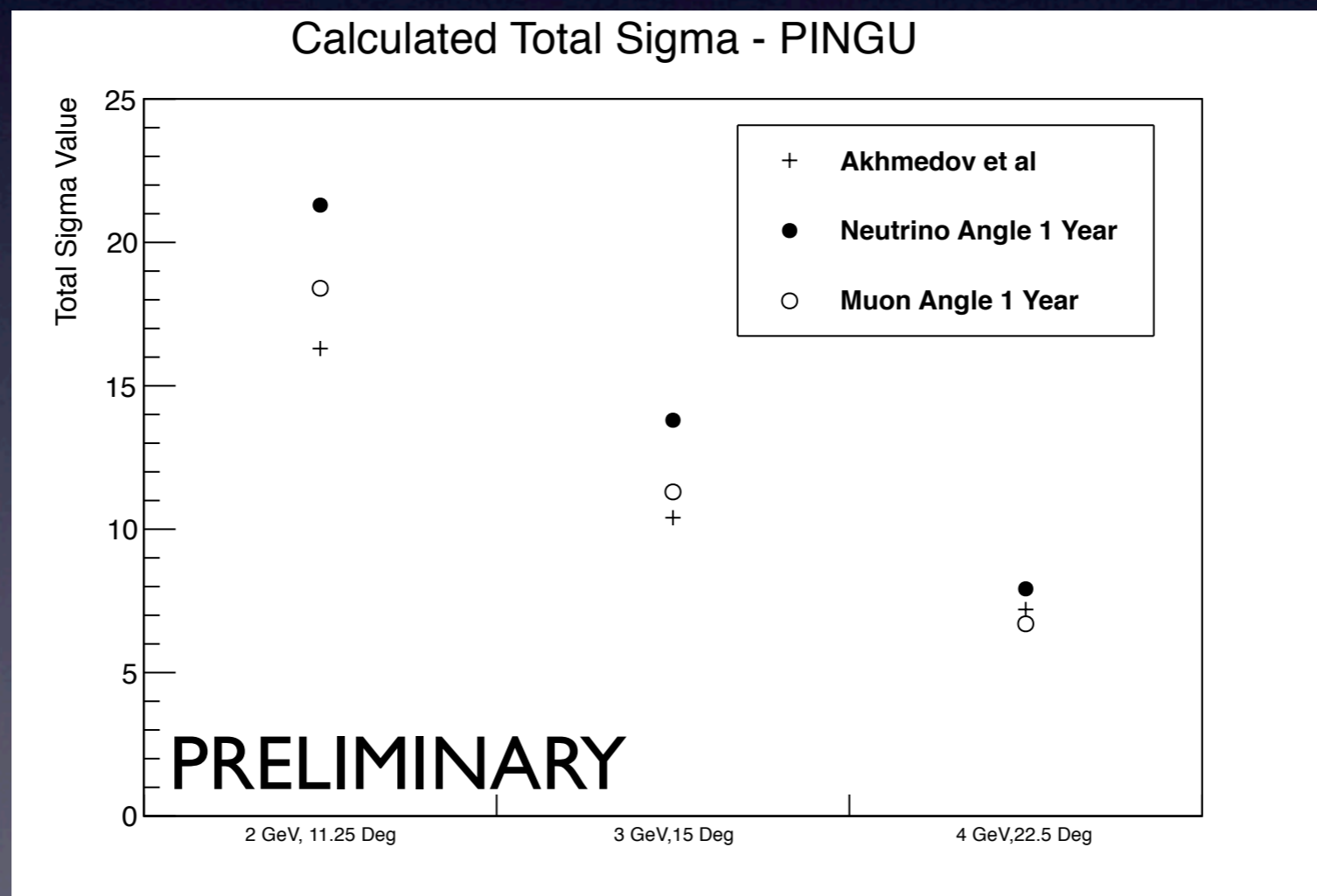


# Detector Resolution



# Comparisons

- Following model in publication, used three different resolution pairs
- $(2\text{GeV}, 11.25^\circ), (3\text{GeV}, 15^\circ), (4\text{GeV}, 22.5^\circ)$

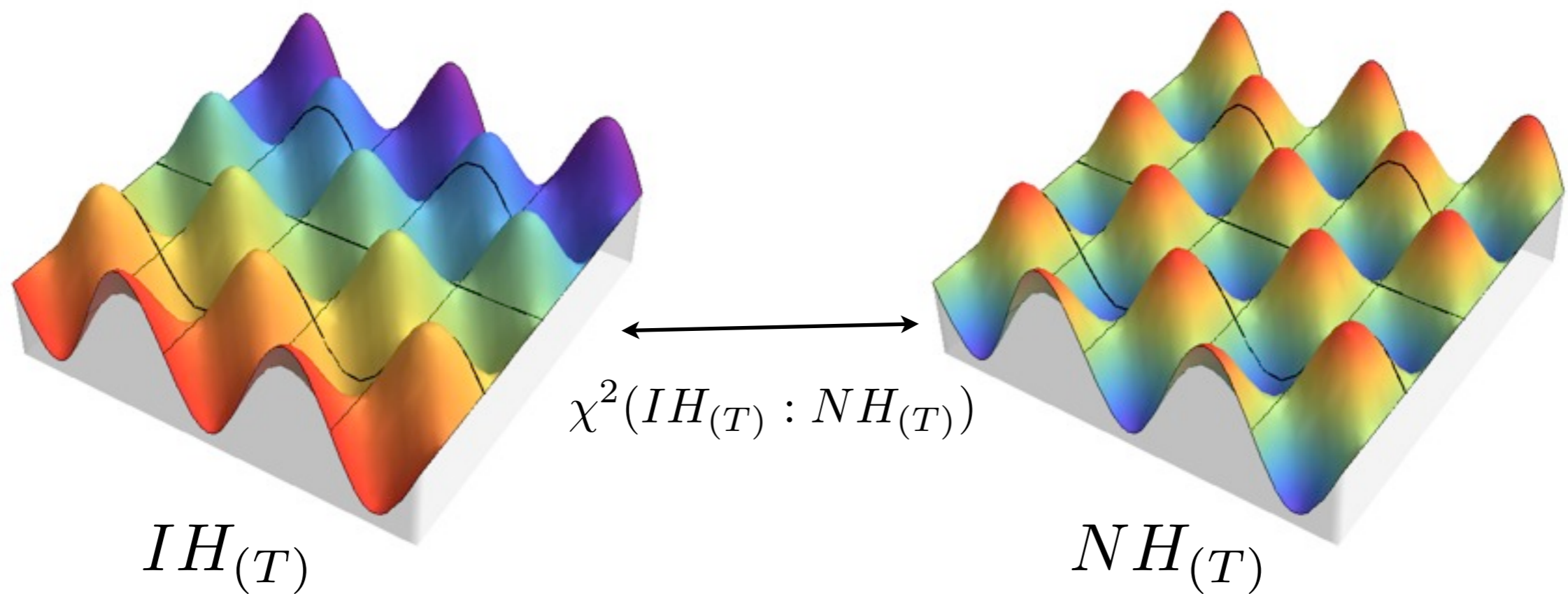


# Systematics

- Studied several effects
  1. Systematic energy shift  $\pm 5\%$ ,  $\pm 10\%$
  2. Systematic angle broadening  $\pm 5\%$ ,  $\pm 10\%$
  3. PREM quantities incorrect
    - Core radii  $\pm 5\%$ ,  $\pm 10\%$
    - Core densities  $\pm 5\%$ ,  $\pm 10\%$



# Systematics - Illustrated

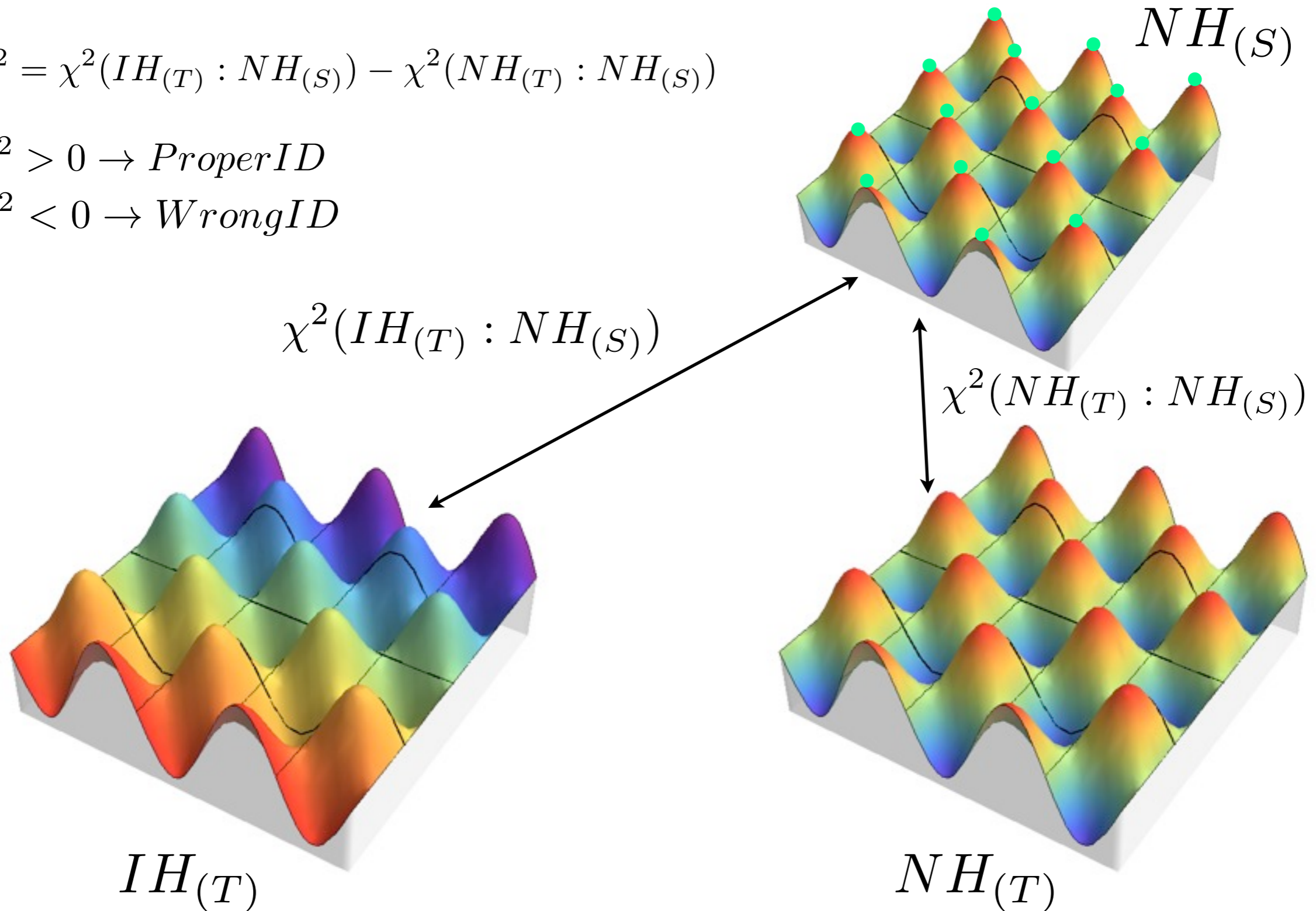


# Systematics - Illustrated

$$\Delta\chi^2 = \chi^2(IH_{(T)} : NH_{(S)}) - \chi^2(NH_{(T)} : NH_{(S)})$$

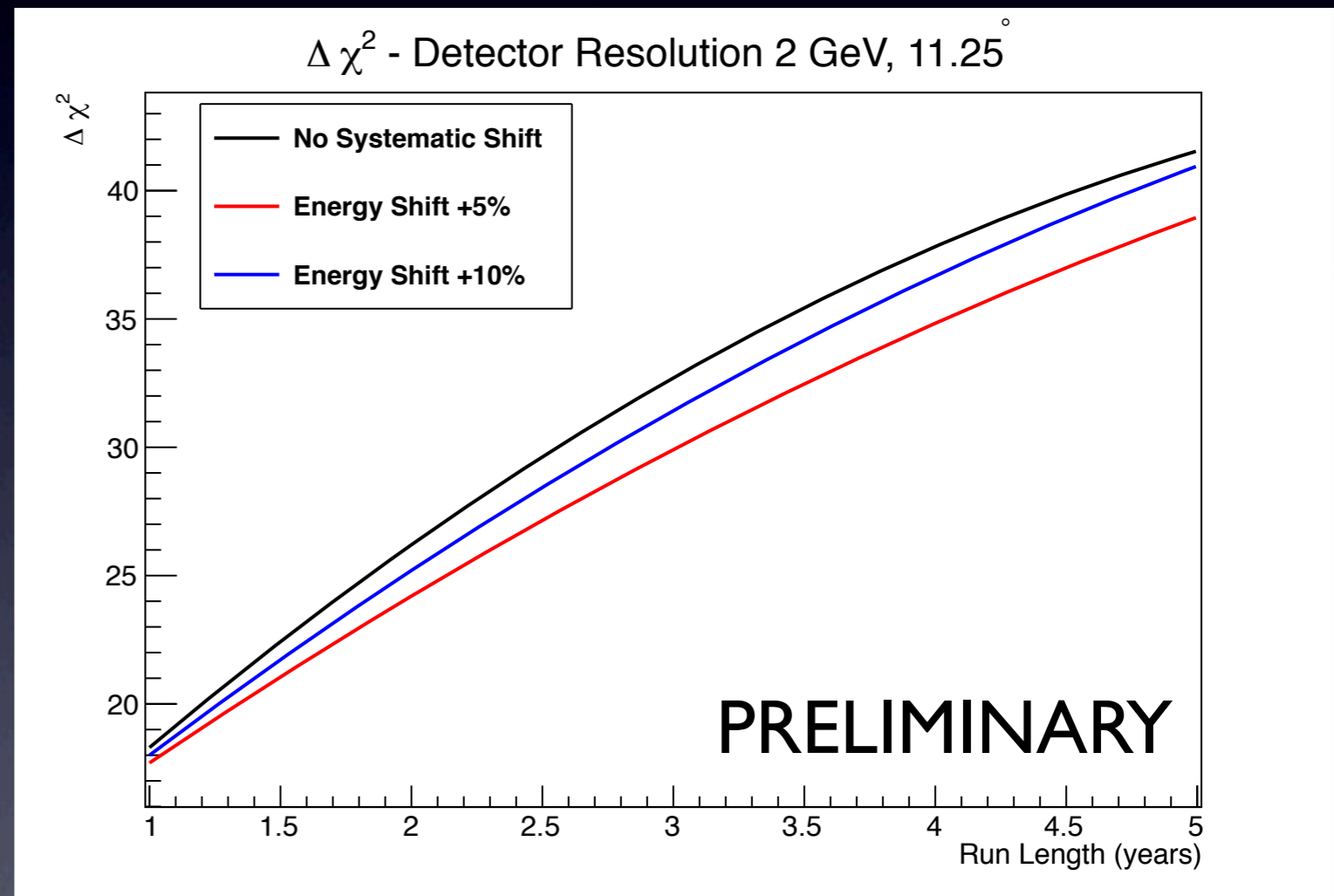
$$\Delta\chi^2 > 0 \rightarrow \textit{ProperID}$$

$$\Delta\chi^2 < 0 \rightarrow \textit{WrongID}$$



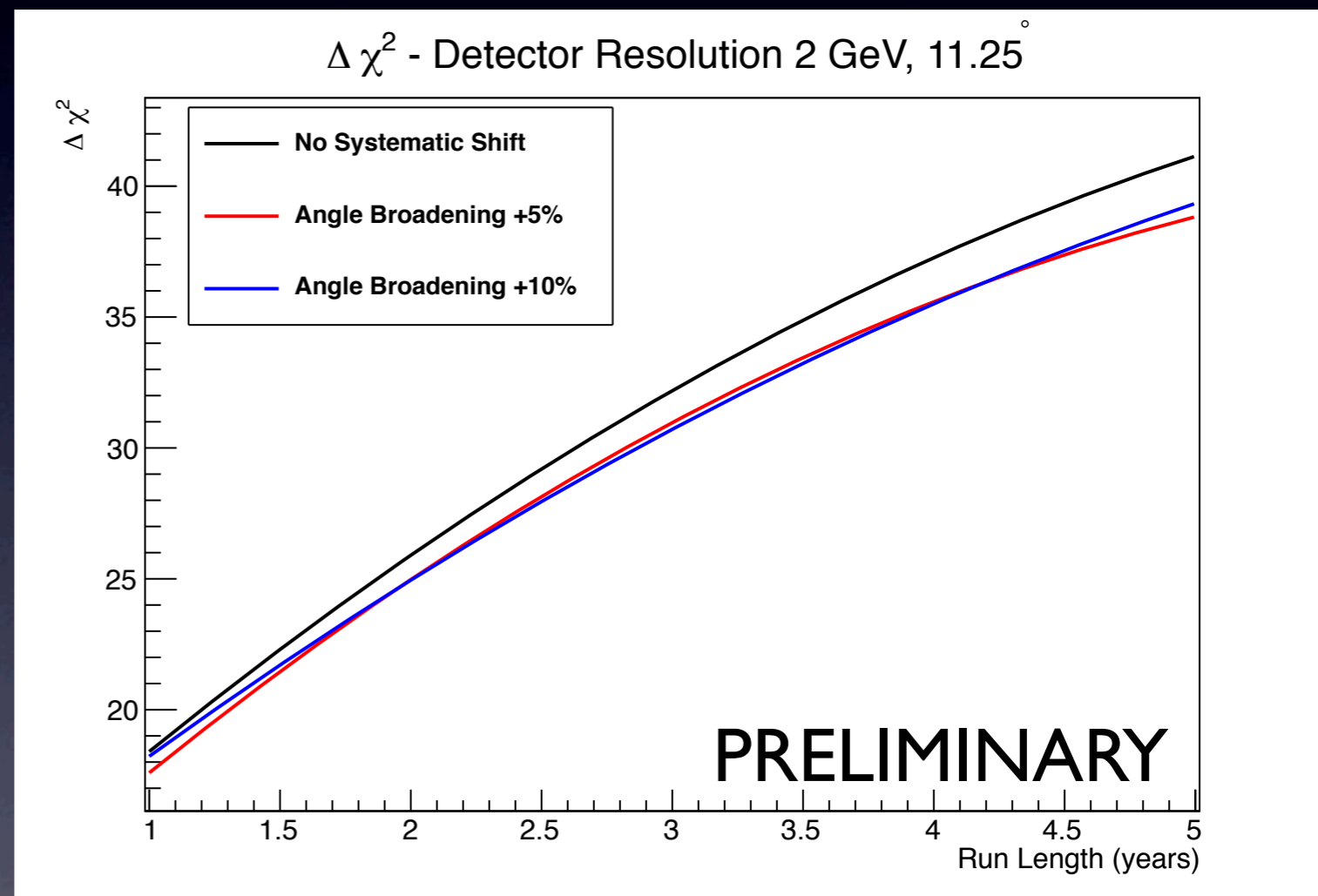
# Energy Shift

- Systematic shift in energy has little effect



# Angle Broadening

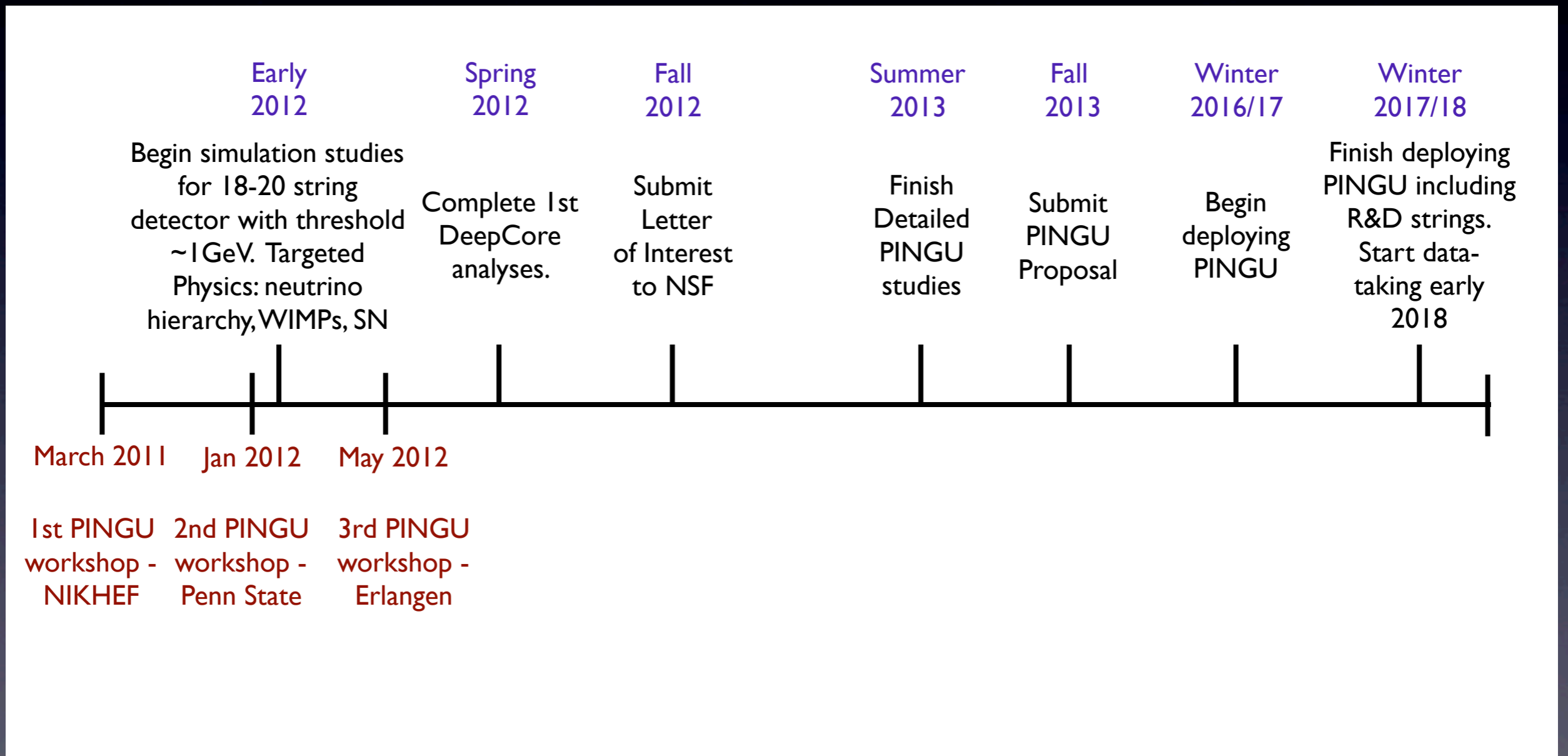
- Not a systematic shift in zenith
- Misunderstanding of the detector resolution



# Next Steps

- Next objective is to include detector resolution effects properly using reconstructions
- Need to perform detailed analysis of systematics
- Start with quantification of best geometry

# Timescale



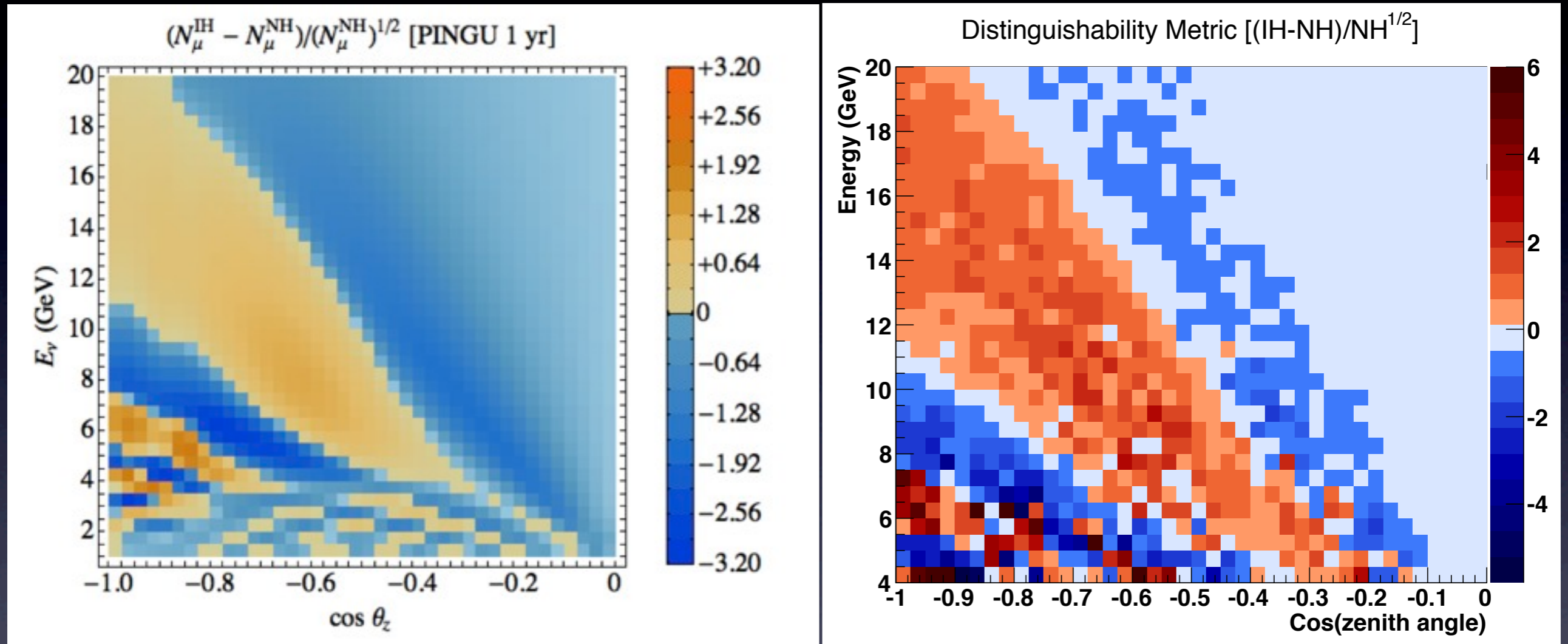
# Conclusion

- Determination of the neutrino mass hierarchy with atmospheric neutrinos appears feasible
- PINGU allows for this determination quickly in a cost effective implementation





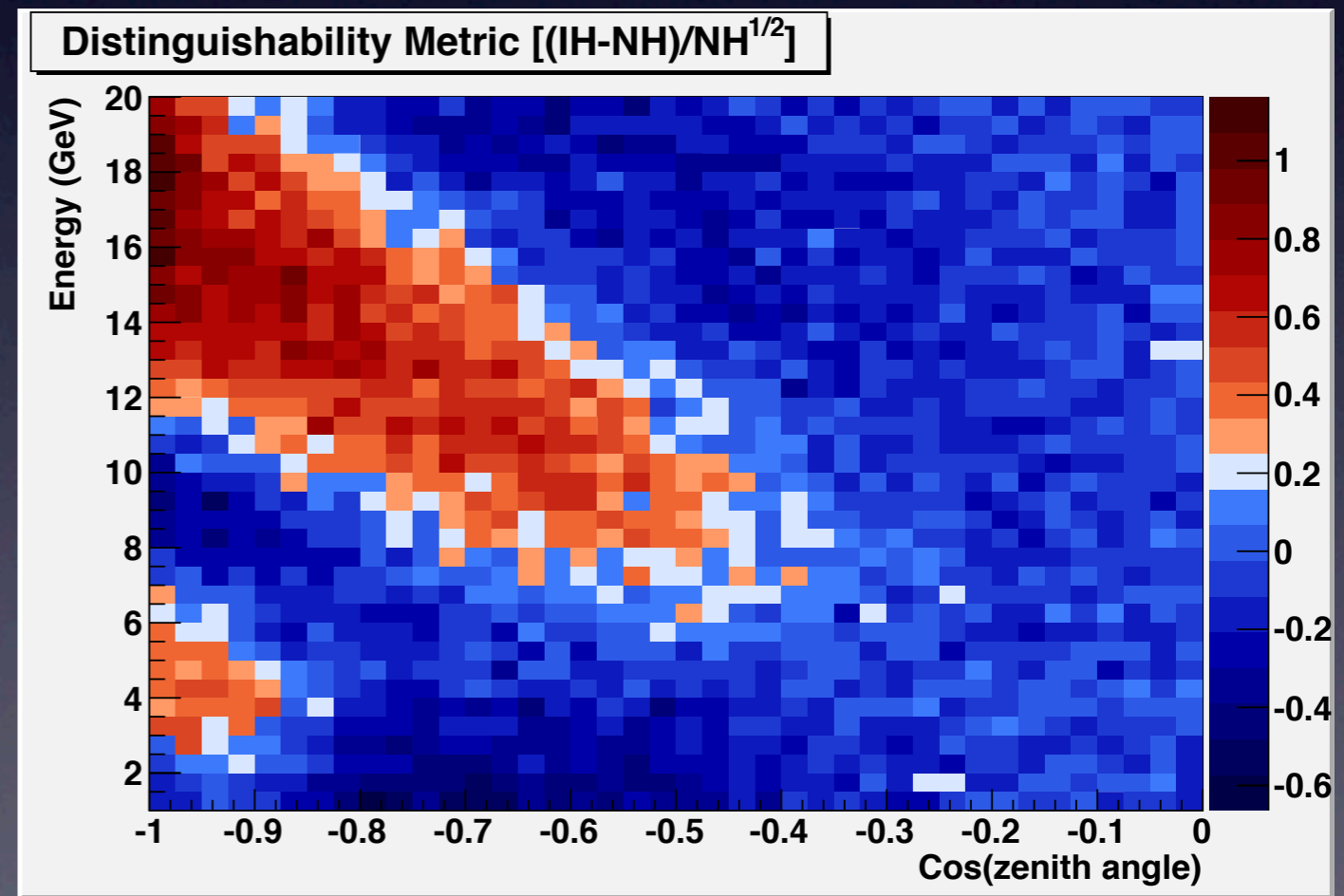
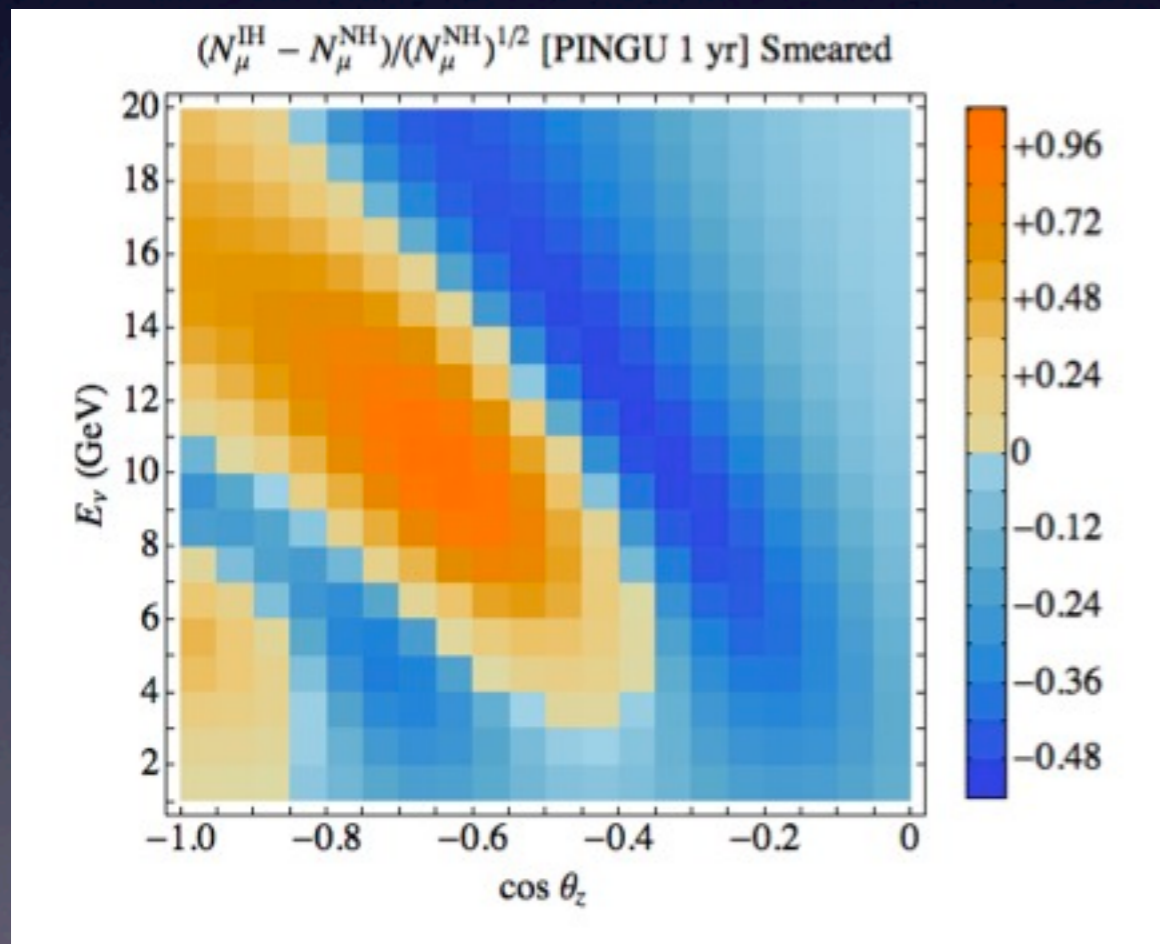
# Comparison



Things seem to compare reasonably well

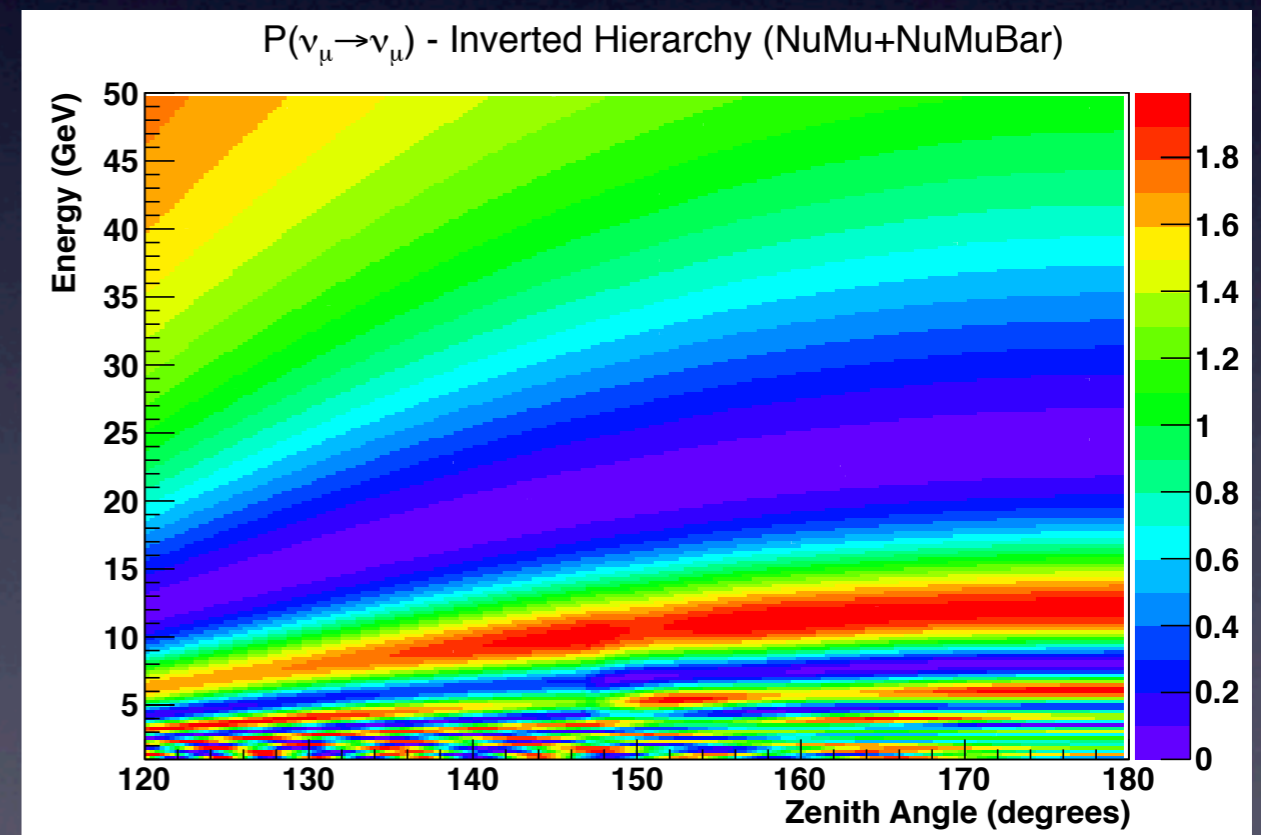
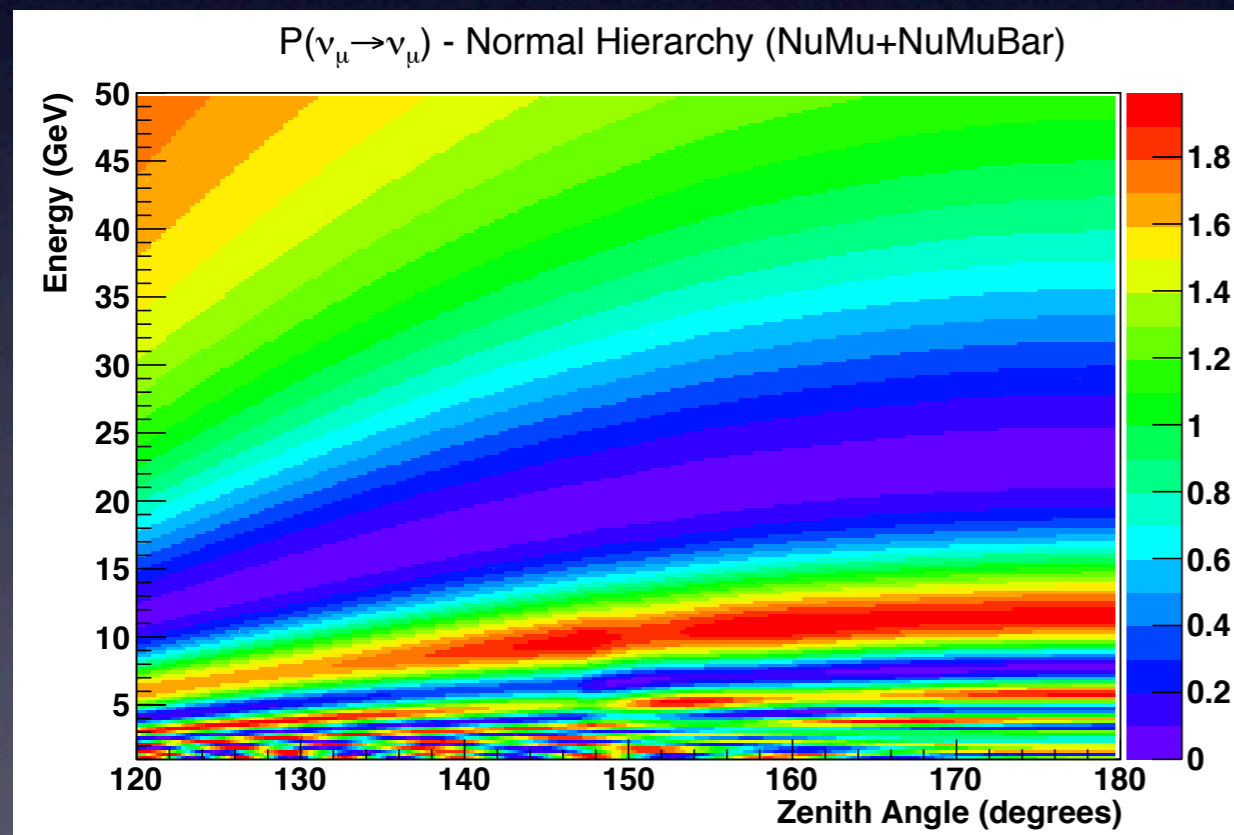
# Detector Resolution Plots

- Shown with detector resolution 2 GeV,  $11.25^\circ$



# Reality(-ish)

- For  $\nu_\mu$ -like events we really get a mixture of  $\nu_\mu$  and  $\bar{\nu}_\mu$



# Systematics

- Can also add systematics on the simulated data:
  1. Apply detector resolution to both hierarchies (IH and NH)
  2. Copy both hierarchies
  3. Apply systematic shift to one copy for each
  4. For each copy, calculate the significance of the opposite unshifted hierarchy and the same unshifted hierarchy
  5. Subtract the same from the opposite value